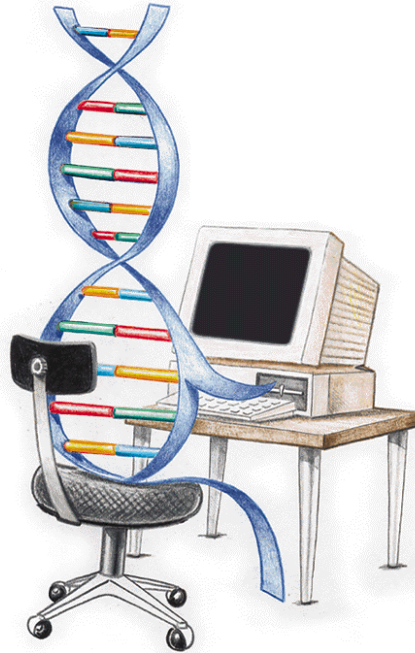


# **AUTOMATED INVENTION BY MEANS OF GENETIC PROGRAMMING**



**AAAI-2004 TUTORIAL—SAN JOSE  
SUNDAY JULY 25, 2004—9AM**

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## THE CHALLENGE

**"How can computers learn to solve problems without being explicitly programmed? In other words, how can computers be made to do what is needed to be done, without being told exactly how to do it?"**

**— Attributed to Arthur Samuel (1959)**

## CRITERION FOR SUCCESS

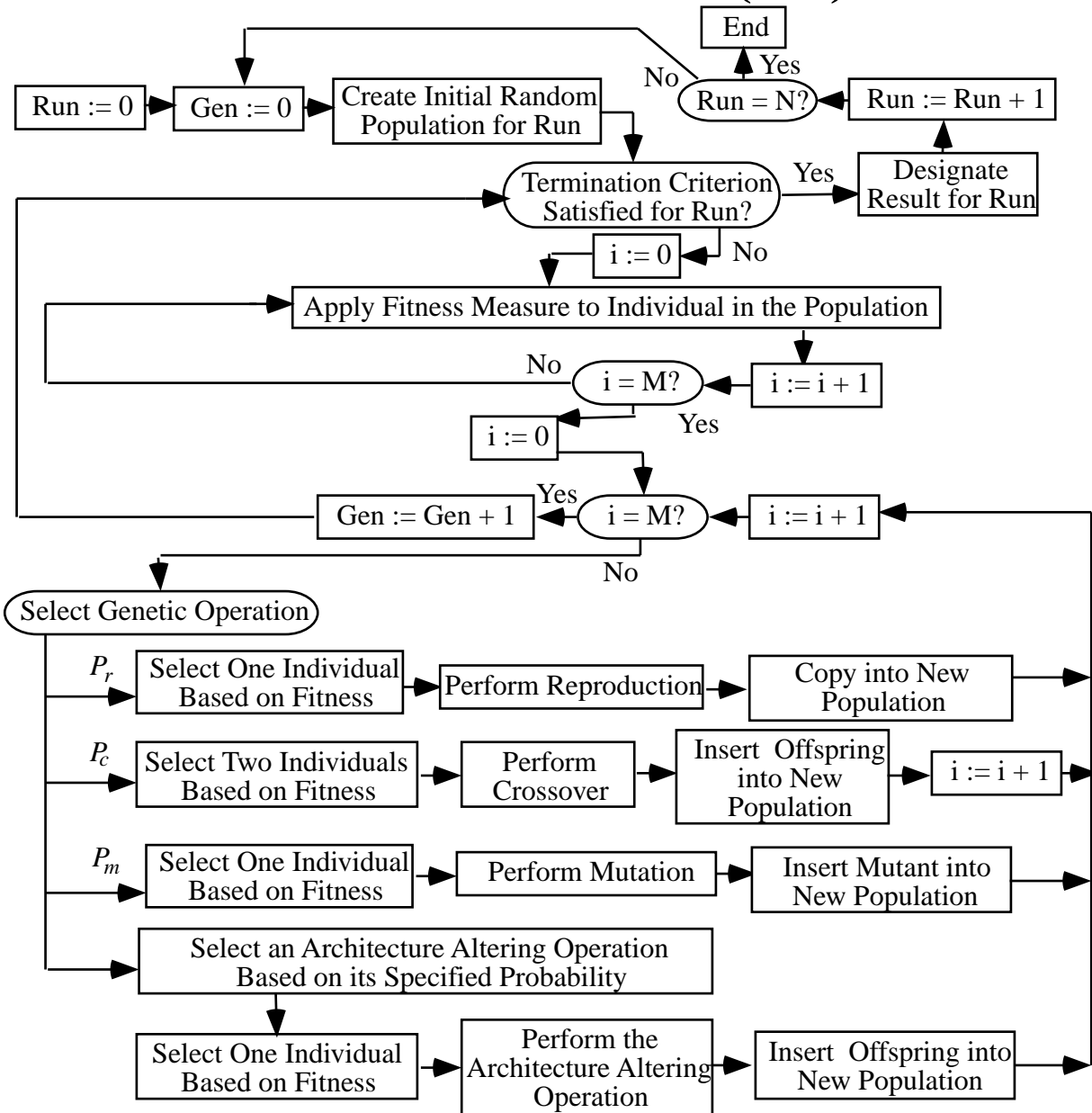
**"The aim [is] ... to get machines to exhibit behavior, which if done by humans, would be assumed to involve the use of intelligence."**

**— Arthur Samuel (1983)**

## MAIN POINTS OF TUTORIAL

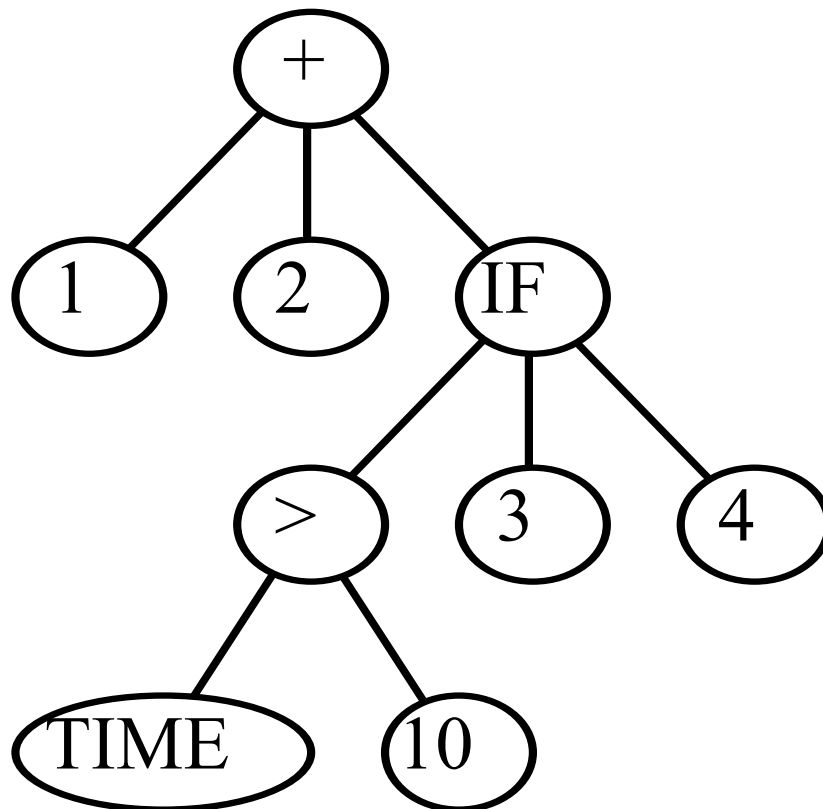
- **Genetic programming now routinely delivers high-return human-competitive machine intelligence**
- **Genetic programming is an automated invention machine**
- **Genetic programming has delivered a progression of qualitatively more substantial results in synchrony with five approximately order-of-magnitude increases in the expenditure of computer time**

# FLOWCHART FOR GENETIC PROGRAMMING (GP)



**COMPUTER PROGRAM  
=PARSE TREE=PROGRAM TREE  
=PROGRAM IN LISP=DATA IN LISP**

- Terminal set  $T = \{1, 2, 10, 3, 4, \text{TIME}\}$
- Function set  $F = \{+, \text{IF}, >\}$

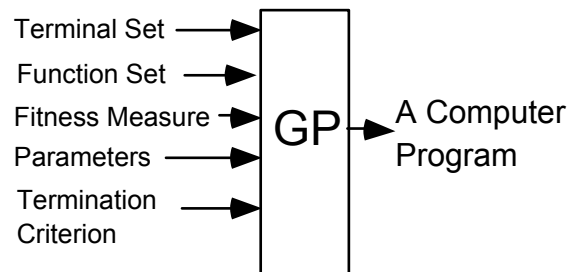


(+ 1 2 (IF (> TIME 10) 3 4))

- Creation of initial population (**GIF**)
- Reproduction operation
- Mutation operation (**GIF**)
- Crossover (recombination) operation (**GIF**)

## FIVE MAJOR PREPARATORY STEPS FOR GP

- **Determining the set of terminals**
- **Determining the set of functions**
- **Determining the fitness measure**
- **Determining the parameters for the run**
  - population size
  - number of generations
  - minor parameters
- **Determining the method for designating a result and the criterion for terminating a run**

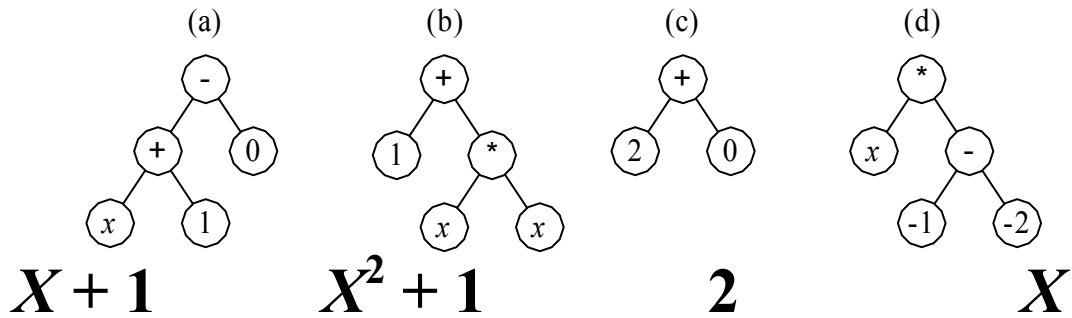


## TABLEAU FOR SYMBOLIC REGRESSION OF QUADRATIC POLYNOMIAL $x^2 + x + 1$

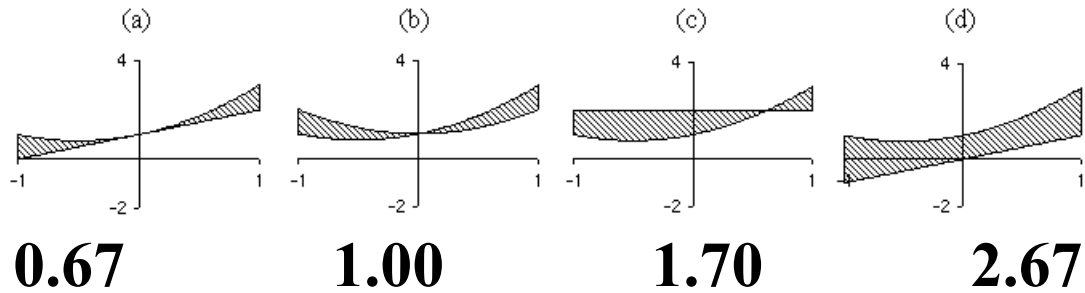
	<b>Objective:</b>	Find a computer program with one input (independent variable $x$ ), whose output equals the value of the quadratic polynomial $x^2 + x + 1$ in range from -1 to +1.
1	<b>Terminal set:</b>	$\mathbf{T} = \{x\}$
2	<b>Function set:</b>	$\mathbf{F} = \{+, -, *, \%\}$ NOTE: The protected division function % returns a value of 1 when division by 0 is attempted (including 0 divided by 0)
3	<b>Fitness:</b>	The sum of the absolute value of the differences (errors), computed (in some way) over values of the independent variable $x$ from -1.0 to +1.0, between the program's output and the target quadratic polynomial $x^2 + x + 1$ .
4	<b>Parameters:</b>	Population size $M = 4$ .
5	<b>Termination:</b>	An individual emerges whose sum of absolute errors is less than 0.1

# SYMBOLIC REGRESSION OF QUADRATIC POLYNOMIAL $X^2 + X + 1$

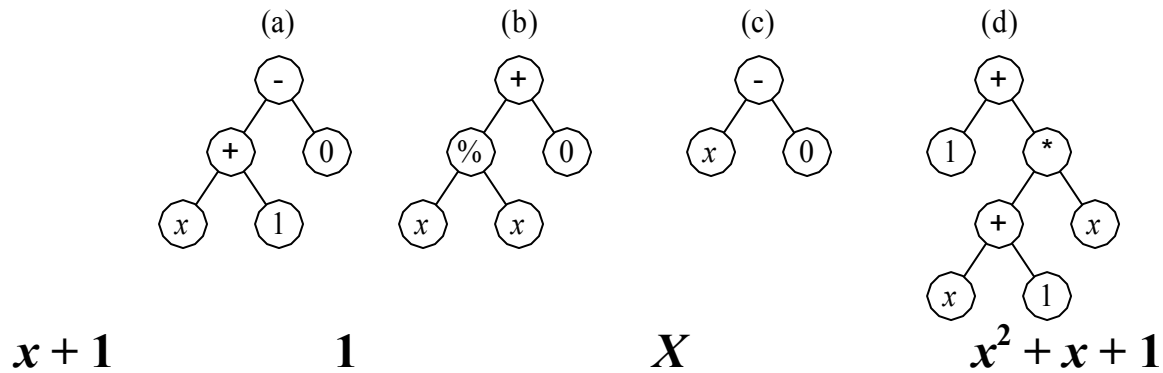
## INITIAL POPULATION—GENERATION 0



## FITNESS



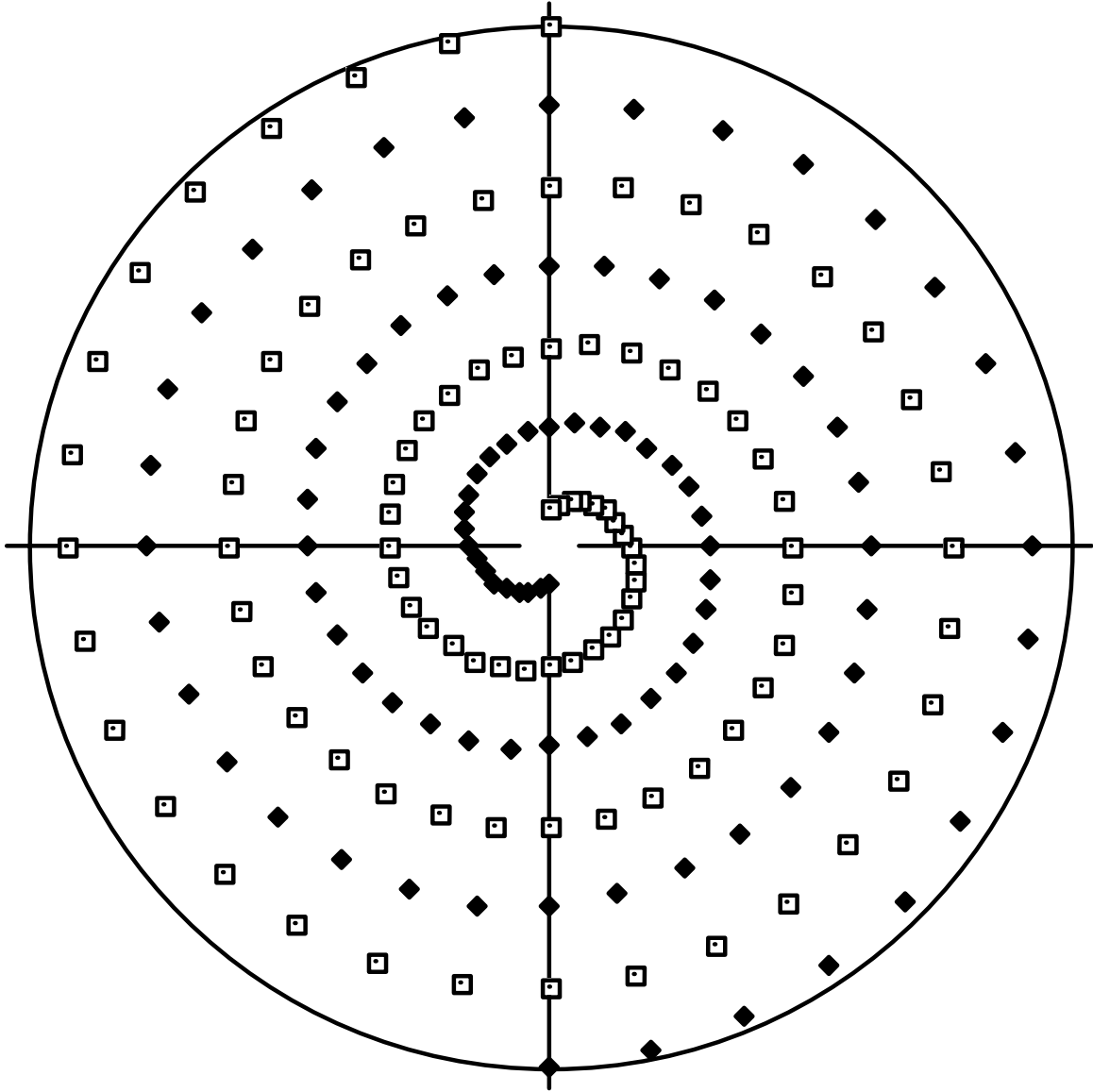
## GENERATION 1



<b>Copy of (a)</b>	<b>Mutant of (c)</b>	<b>First</b>	<b>Second</b>
	—picking “2” as mutation point	offspring of crossover (a) and (b)	offspring of crossover (a) and (b)
		—picking “+” of parent (a) and left-most “x” of parent (b) as crossover points	—picking “+” of parent (a) and left-most “x” of parent (b) as crossover points



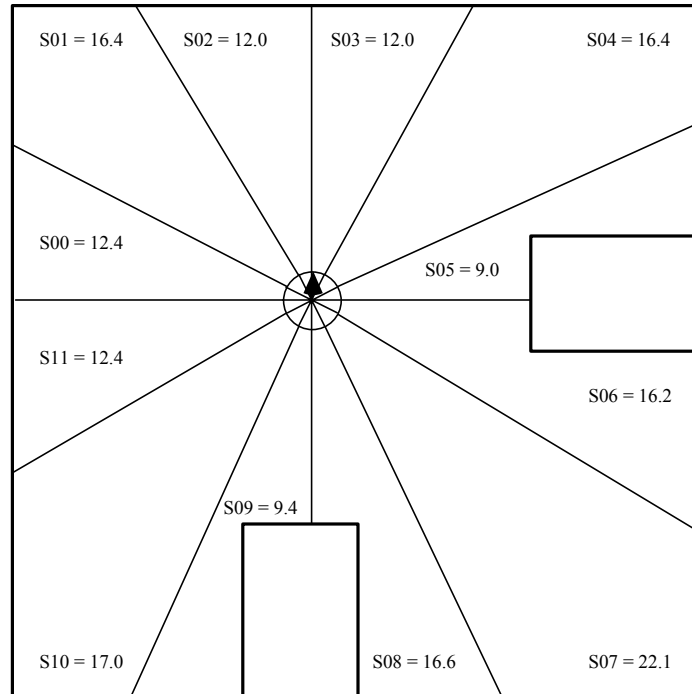
# CLASSIFICATION PROBLEM INTER-TWINED SPIRALS



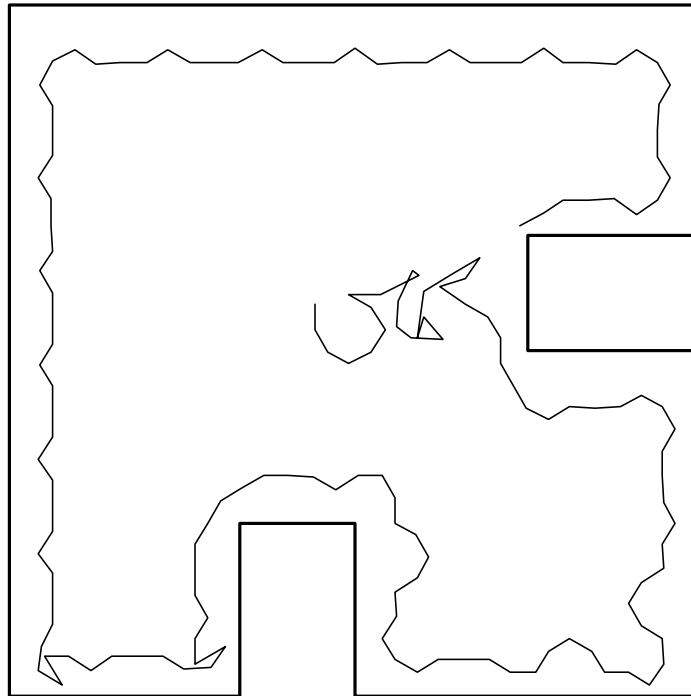
## GP TABLEAU – INTERTWINED SPIRALS

<b>Objective:</b>	Find a program to classify a given point in the $x$ - $y$ plane to the red or blue spiral.
<b>Terminal set:</b>	$x$ , $y$ , $\mathfrak{R}$ , where $\mathfrak{R}$ is the ephemeral random floating-point constant ranging between $-1.000$ and $+1.000$ .
<b>Function set:</b>	$+$ , $-$ , $*$ , $\%$ , IFLTE, SIN, COS.
<b>Fitness cases:</b>	194 points in the $x$ - $y$ plane.
<b>Raw fitness:</b>	The number of correctly classified points (0 – 194)
<b>Standardized fitness:</b>	The maximum raw fitness (i.e., 194) minus the raw fitness.
<b>Hits:</b>	Equals raw fitness.
<b>Wrapper:</b>	Maps any individual program returning a positive value to class +1 (red) and maps all other values to class $-1$ (blue).
<b>Parameters:</b>	$M = 10,000$ (with over-selection). $G = 51$ .
<b>Success predicate:</b>	An individual program scores 194 hits.

# WALL-FOLLOWING PROBLEM



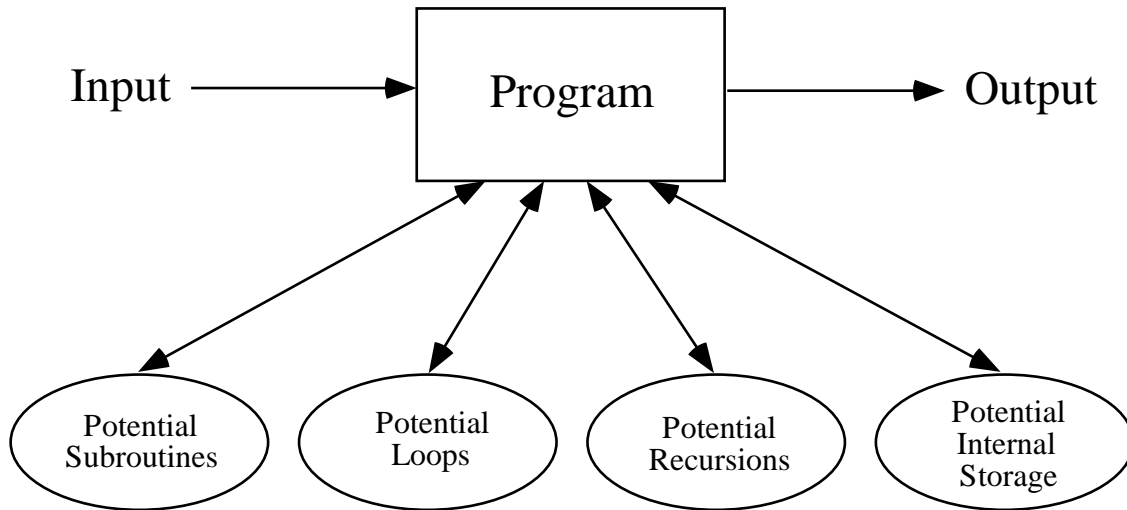
## EVOLVED WALL-FOLLOWER



## **SOME OF THE PROBLEMS SOLVED IN *GENETIC PROGRAMMING* (KOZA 1992)**

- **Symbolic Regression**
- **Intertwined Spirals**
- **Wall Following**
- **Box Moving**
- **Truck Backer Upper**
- **Broom Balancing**
- **Artificial Ant**
- **Discrete Pursuer-Evader Game**
- **Differential Pursuer-Evader Game**
- **Co-Evolution of Game-Playing Strategies**
- **Inverse Kinematics**
- **Emergent Collecting**
- **Central Place Foraging**
- **Block Stacking**
- **Randomizer**
- **1-D Cellular Automata**
- **2-D Cellular Automata**
- **Task Prioritization**
- **Programmatic Image Compression**
- **Finding  $3\sqrt{2}$**
- **Econometric Exchange Equation**
- **Optimization (Lizard)**
- **Boolean 11-Multiplexer**
- **11-Parity–Automatically Defined Functions**

# AUTOMATICALLY DEFINED FUNCTIONS (ADFs, SUBROUTINES)

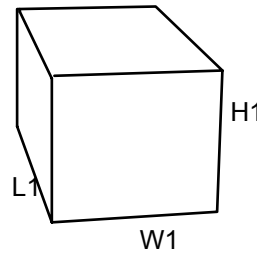
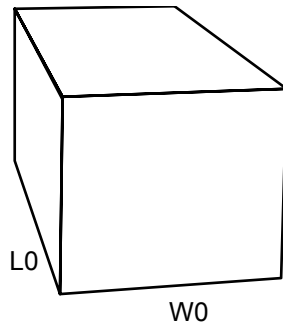


- **Subroutines provide one way to REUSE code — possibly with different instantiations of the dummy variables (formal parameters)**
- **Loops (and iterations) provide a 2<sup>nd</sup> way to REUSE code**
- **Recursion provide a 3<sup>rd</sup> way to REUSE code**
- **Memory provides a 4<sup>th</sup> way — to REUSE the results of executing code**

# AUTOMATICALLY DEFINED FUNCTIONS (ADFs, SUBROUTINES)

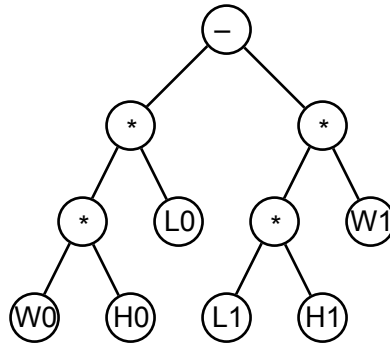
**10 FITNESS-CASES SHOWING THE  
VALUE OF THE DEPENDENT  
VARIABLE,  $D$ , ASSOCIATED WITH THE  
VALUES OF THE SIX INDEPENDENT  
VARIABLES,  $L_0, W_0, H_0, L_1, W_1, H_1$**

<b>Fitness case</b>	$L_0$	$W_0$	$H_0$	$L_1$	$W_1$	$H_1$	<b>Dependent variable <math>D</math></b>
<b>1</b>	3	4	7	2	5	3	<b>54</b>
<b>2</b>	7	10	9	10	3	1	<b>600</b>
<b>3</b>	10	9	4	8	1	6	<b>312</b>
<b>4</b>	3	9	5	1	6	4	<b>111</b>
<b>5</b>	4	3	2	7	6	1	<b>-18</b>
<b>6</b>	3	3	1	9	5	4	<b>-171</b>
<b>7</b>	5	9	9	1	7	6	<b>363</b>
<b>8</b>	1	2	9	3	9	2	<b>-36</b>
<b>9</b>	2	6	8	2	6	10	<b>-24</b>
<b>10</b>	8	1	10	7	5	1	<b>45</b>



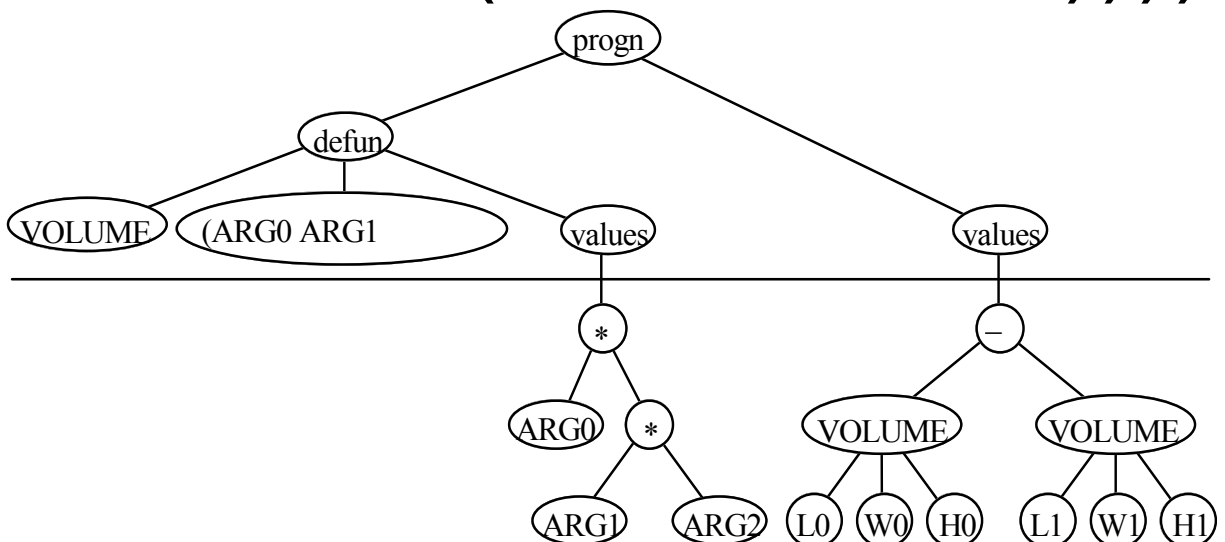
## SOLUTION WITHOUT ADFs

```
(- (* (* W0 L0) H0)
   (* (* W1 L1) H1))
```



## SOLUTION WITH ADFs

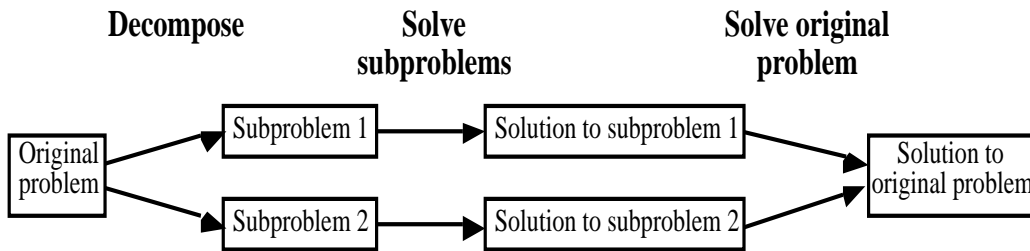
```
(progn
  (defun volume (arg0 arg1 arg2)
    (values
      (* arg0 (* arg1 arg2))))
  (values (- (volume L0 W0 H0)
            (volume L1 W1 H1))))
```



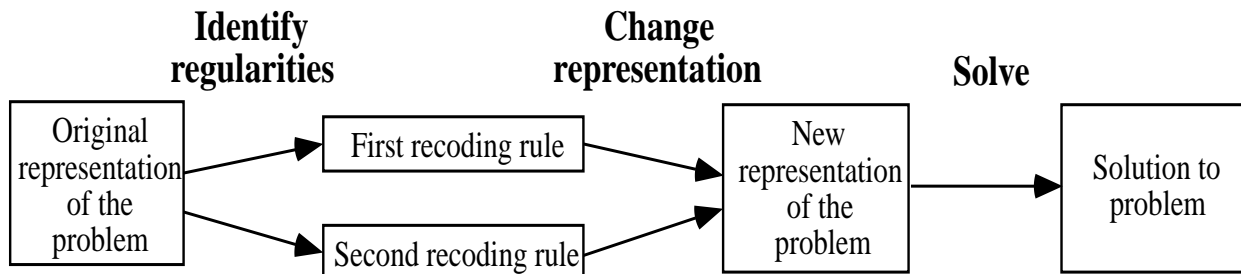
## ADFs (SUBROUTINES)

Fitness case	$L_0$	$W_0$	$H_0$	$L_1$	$W_1$	$H_1$	$V_0$	$V_1$	$D$
<b>1</b>	3	4	7	2	5	3	<b>84</b>	<b>30</b>	<b>54</b>
<b>2</b>	7	10	9	10	3	1	<b>630</b>	<b>30</b>	<b>600</b>
<b>3</b>	10	9	4	8	1	6	<b>360</b>	<b>48</b>	<b>312</b>
<b>4</b>	3	9	5	1	6	4	<b>135</b>	<b>24</b>	<b>111</b>
<b>5</b>	4	3	2	7	6	1	<b>24</b>	<b>42</b>	<b>-18</b>
<b>6</b>	3	3	1	9	5	4	<b>9</b>	<b>180</b>	<b>-171</b>
<b>7</b>	5	9	9	1	7	6	<b>405</b>	<b>42</b>	<b>363</b>
<b>8</b>	1	2	9	3	9	2	<b>18</b>	<b>54</b>	<b>-36</b>
<b>9</b>	2	6	8	2	6	10	<b>96</b>	<b>120</b>	<b>-24</b>
<b>10</b>	8	1	10	7	5	1	<b>80</b>	<b>35</b>	<b>45</b>

### TOP-DOWN VIEW



### BOTTOM-UP VIEW





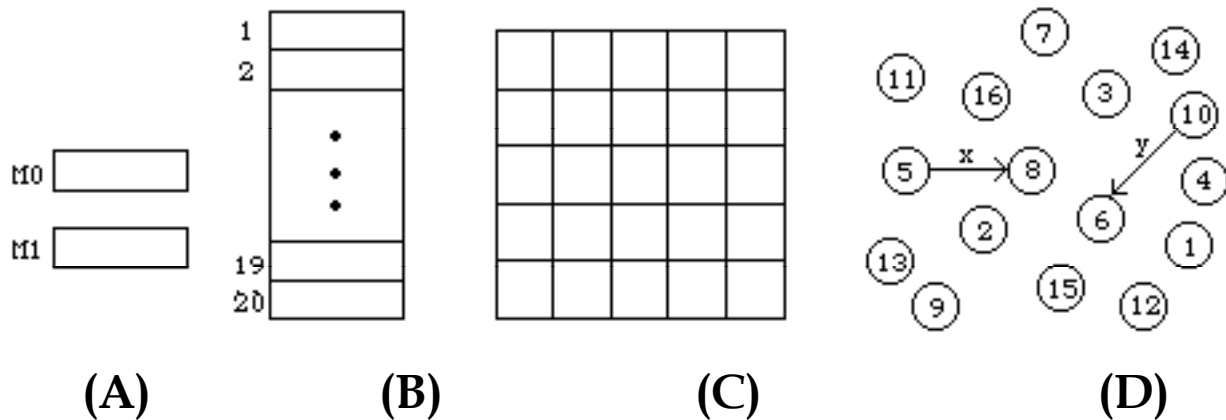
# **AUTOMATICALLY DEFINED FUNCTIONS (ADFs, SUBROUTINES)**

## **8 MAIN POINTS FROM BOOK *GENETIC PROGRAMMING II: AUTOMATIC DISCOVERY OF REUSABLE PROGRAMS (KOZA 1994)***

- **ADFs work.**
- **ADFs do not solve problems in the style of human programmers.**
- **ADFs reduce the computational effort required to solve a problem.**
- **ADFs usually improve the parsimony of the solutions to a problem.**
- **As the size of a problem is scaled up, the size of solutions increases more slowly with ADFs than without them.**
- **As the size of a problem is scaled up, the computational effort required to solve a problem increases more slowly with ADFs than without them.**
- **The advantages in terms of computational effort and parsimony conferred by ADFs increase as the size of the problem is scaled up.**

# REUSE

## MEMORY AND STORAGE



- (A) Settable (named) variables (*Genetic Programming*, Koza 1992) using setting (writing) functions (`SETM0 X`) and (`SETM1 Y`) and reading by means of terminals `M0` and `M1`.
- (B) Indexed memory similar to linear (vector) computer memory (Teller 1994) using (`READ K`) and (`WRITE X K`)
- (C) Matrix memory (Andre 1994)
- (D) Relational memory (Brave 1995, 1996)

## LANGDON'S DATA STRUCTURES

- Stacks
- Queues
- Lists
- Rings

# REUSE

## AUTOMATICALLY DEFINED ITERATIONS (ADIs)

### TRANSMEMBRANE SEGMENT IDENTIFICATION PROBLEM

- Goal is to classify a given protein segment as being a transmembrane domain or non-transmembrane domain
- Generation 20 — Run 3 — Subset-creating version
  - in-sample correlation of 0.976
  - out-of-sample correlation of 0.968
  - out-of-sample error rate 1.6%

(progn

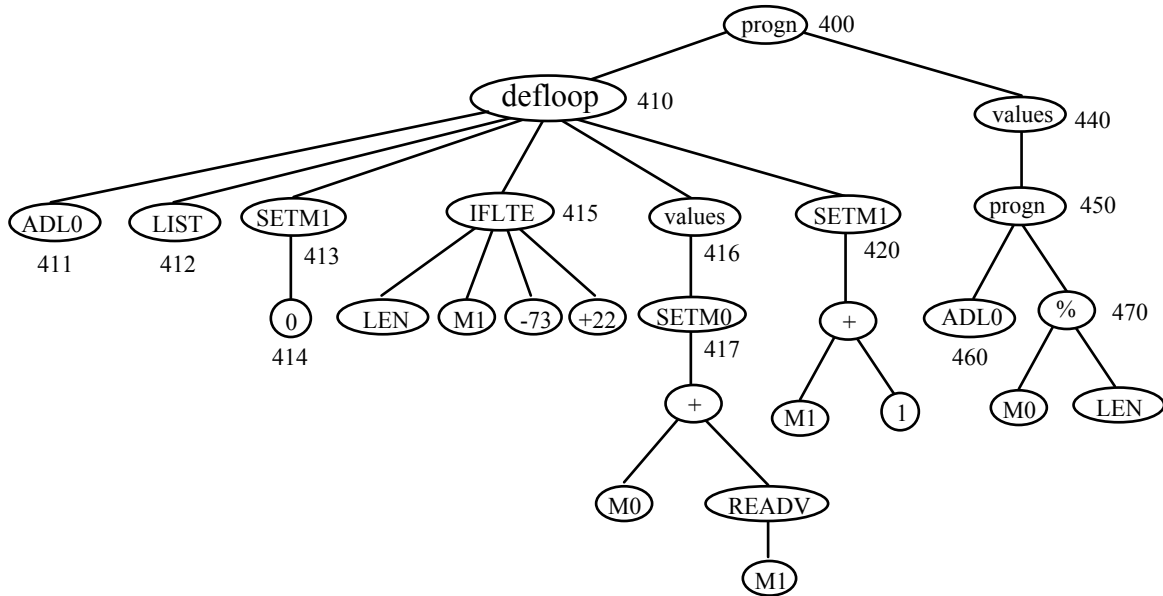
```

  (defun ADF0 ()
    (ORN (ORN (ORN (I?) (H?)) (ORN (P?) (G?))) (ORN (ORN
      (ORN (Y?) (N?)) (ORN (T?) (Q?))) (ORN (A?) (H?))))))
  (defun ADF1 ()
    (values (ORN (ORN (ORN (A?) (I?)) (ORN (L?) (W?)))
      (ORN (ORN (T?) (L?)) (ORN (T?) (W?))))))
  (defun ADF2 ()
    (values (ORN (ORN (ORN (ORN (ORN (D?) (E?)) (ORN (ORN
      (ORN (D?) (E?)) (ORN (ORN (T?) (W?)) (ORN (Q?)
      (D?)))) (ORN (K?) (P?)))) (ORN (K?) (P?)) (ORN (T?)
      (W?)) (ORN (ORN (E?) (A?)) (ORN (N?) (R?))))))
    (progn (loop-over-residues
      (SETM0 (+ (- (ADF1) (ADF2)) (SETM3 M0))))
      (values (% (% M3 M0) (% (% (% (- L -0.53) (* M0
      M0)) (+ (% (% M3 M0) (% (+ M0 M3) (% M1 M2)))) M2)) (%
      M3 M0))))))

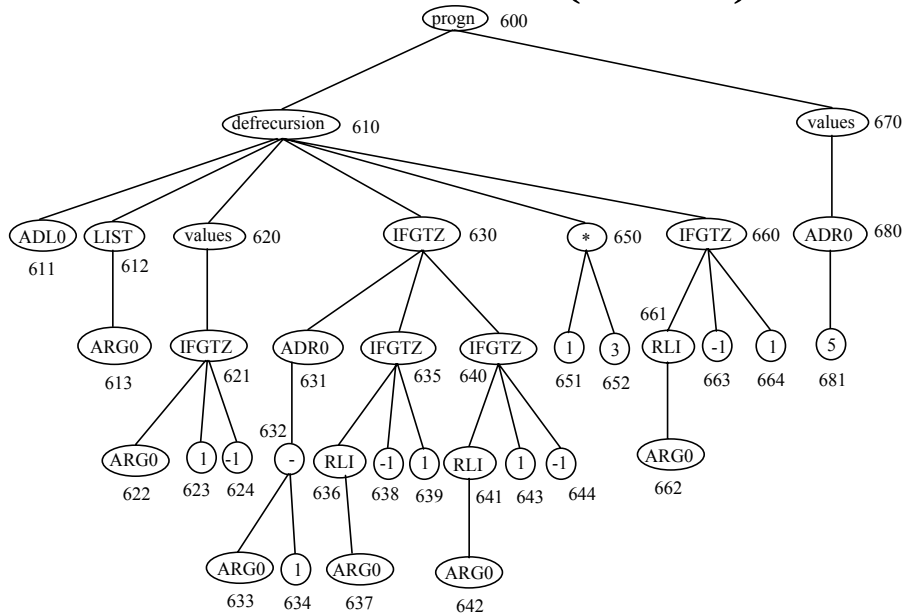
```

# REUSE

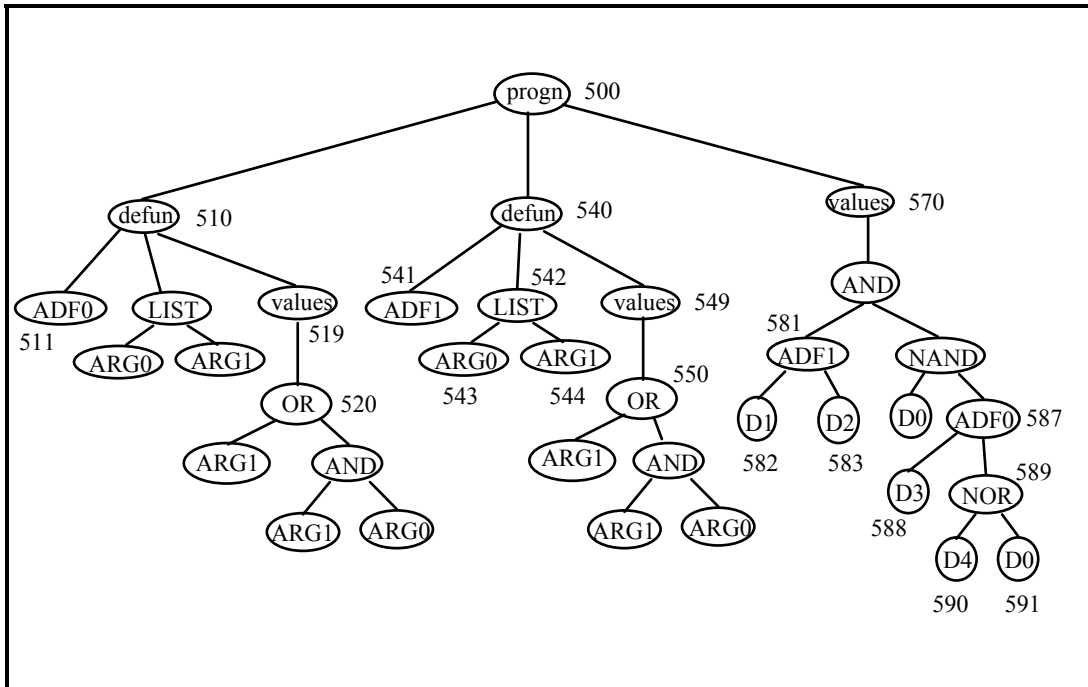
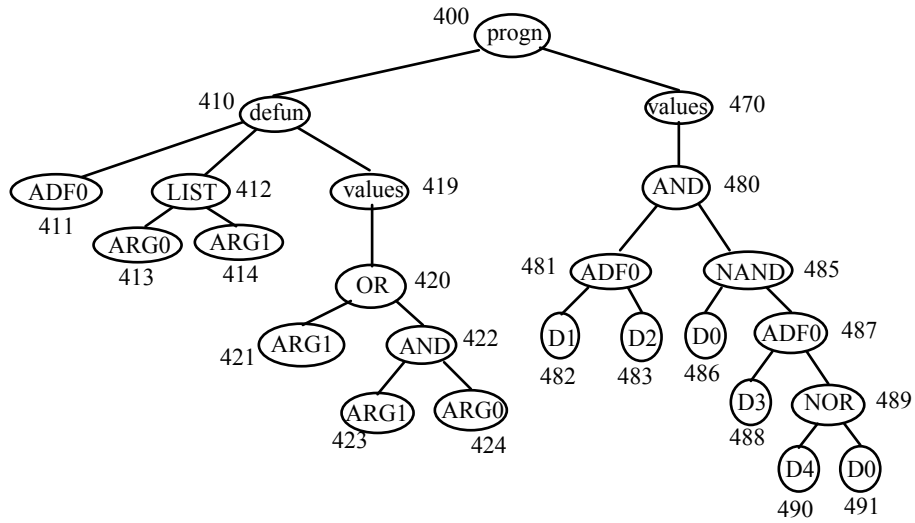
## AUTOMATICALLY DEFINED LOOP (ADL0)



## AUTOMATICALLY DEFINED RECURSION (ADR0)



# ARCHITECTURE-ALTERING OPERATIONS



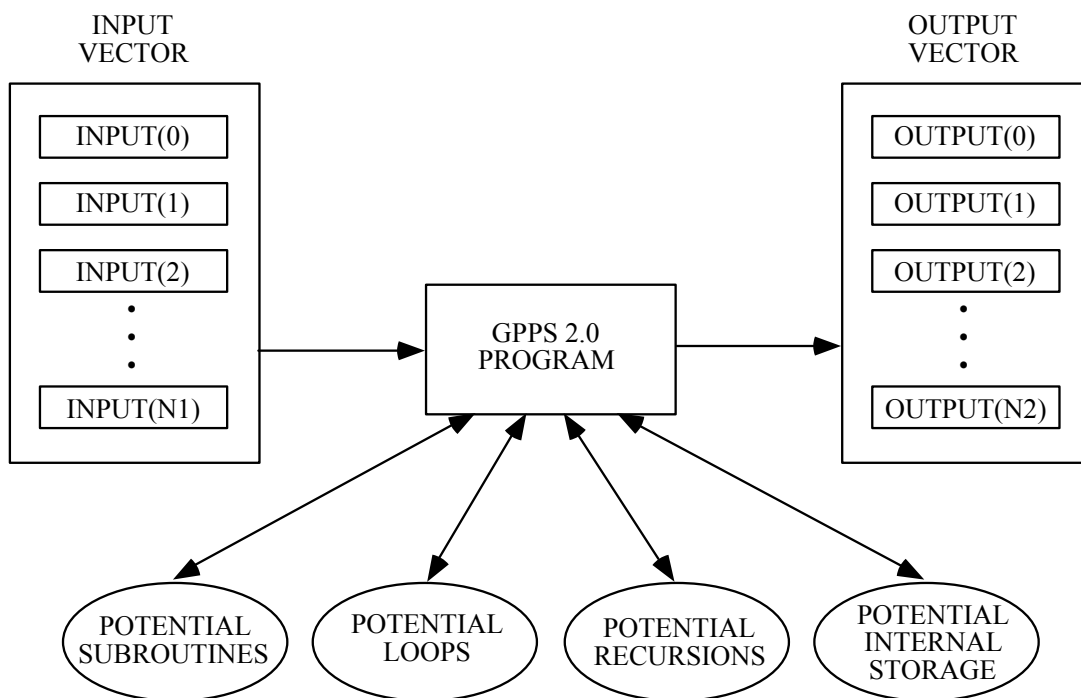
**(GIFS)**

# **16 ATTRIBUTES OF A SYSTEM FOR AUTOMATICALLY CREATING COMPUTER PROGRAMS**

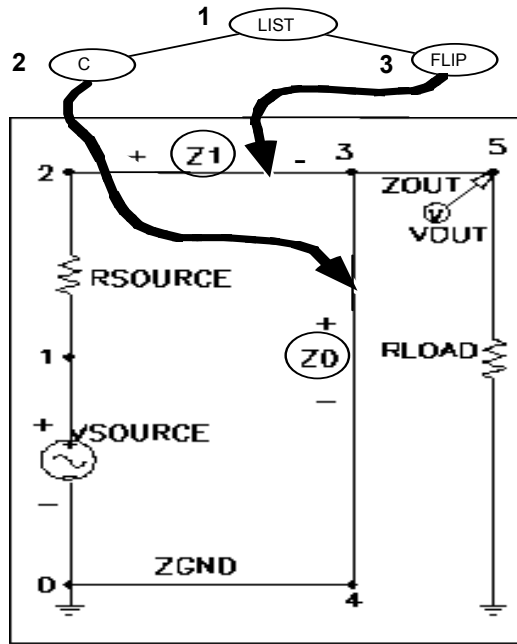
- 1 — Starts with "What needs to be done"**
- 2 — Tells us "How to do it"**
- 3 — Produces a computer program**
- 4 — Automatic determination of program size**
- 5 — Code reuse**
- 6 — Parameterized reuse**
- 7 — Internal storage**
- 8 — Iterations, loops, and recursions**
- 9 — Self-organization of hierarchies**
- 10 — Automatic determination of program architecture**
- 11 — Wide range of programming constructs**
- 12 — Well-defined**
- 13 — Problem-independent**
- 14 — Wide applicability**
- 15 — Scalable**
- 16 — Competitive with human-produced results**

# ARCHITECTURE-ALTERING OPERATIONS

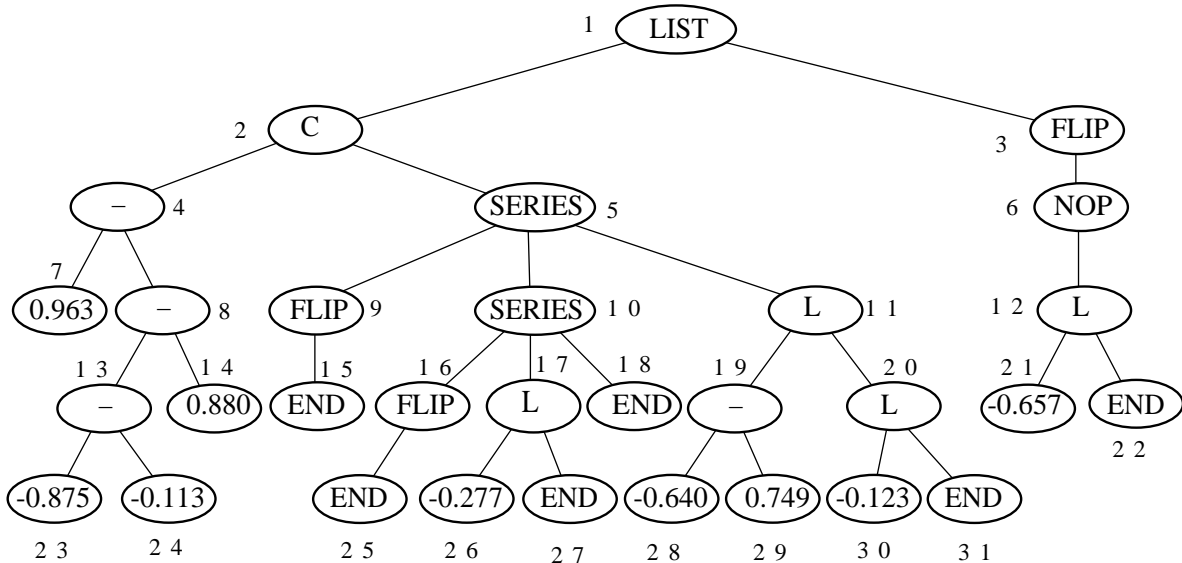
## GENETIC PROGRAMMING PROBLEM SOLVER (GPPS) — VERSION 2.0



# DEVELOPMENTAL GP

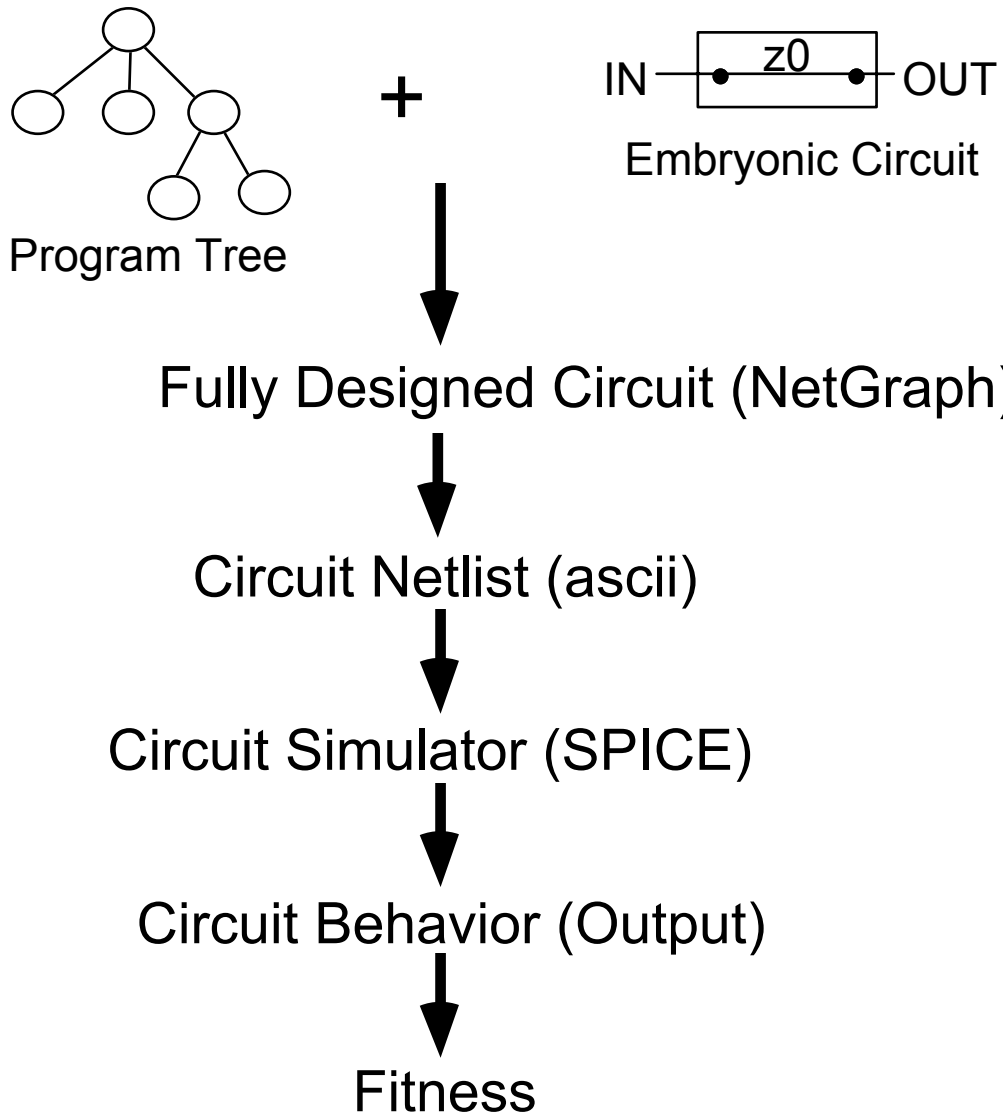


```
(LIST (C (- 0.963 (- (- -0.875 -0.113)
0.880)) (series (flip end) (series (flip
end) (L -0.277 end) end) (L (- -0.640
0.749) (L -0.123 end)))) (flip (nop (L -
0.657 end))))))
```

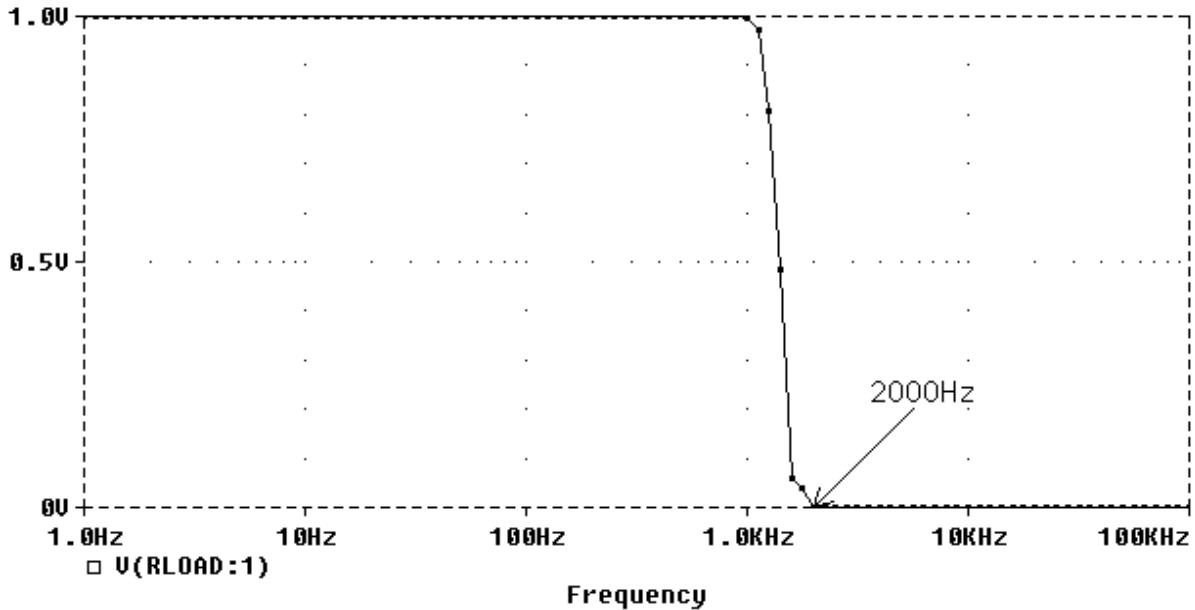




# EVALUATION OF FITNESS OF A CIRCUIT

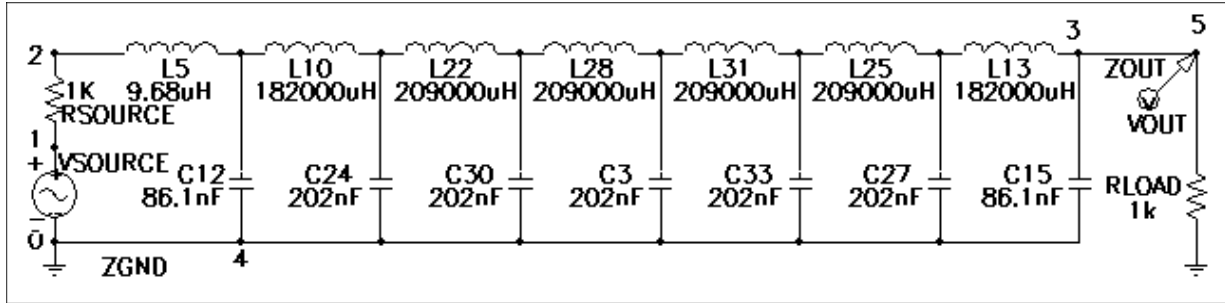


## BEHAVIOR OF A LOWPASS FILTER VIEWED IN THE FREQUENCY DOMAIN

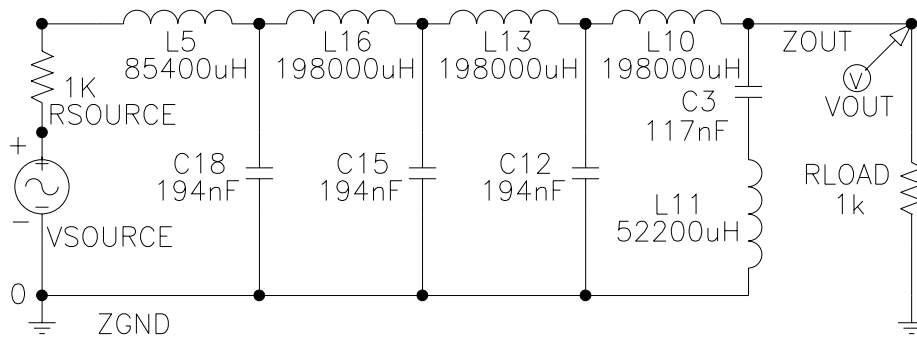


- Examine circuit's behavior for each of 101 frequency values chosen over five decades of frequency (from 1 Hz to 100,000 Hz) with each decade divided into 20 parts (using a logarithmic scale). The fitness measure
  - does not penalize ideal values
  - slightly penalizes acceptable deviations
  - heavily penalizes unacceptable deviations
- Fitness is sum  $F(t) = \sum_{i=0}^{100} [W(f_i)d(f_i)]$ 
  - $f(i)$  is the frequency of fitness case  $i$
  - $d(x)$  is the difference between the target and observed values at frequency of fitness case  $i$
  - $W(y,x)$  is the weighting at frequency  $x$

**EVOLVED FILTER**  
**U. S. PATENT 1,227,113—GEORGE**  
**CAMPBELL—AT&T—1917**

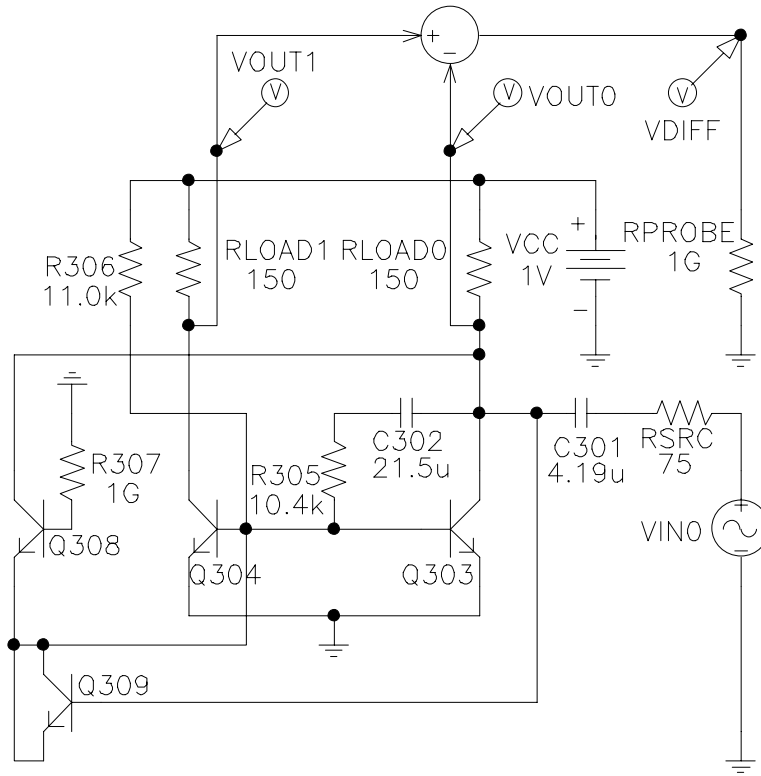


**EVOLVED FILTER**  
**U. S. PATENT 1,538,964—OTTO ZOBEL—**  
**AT&T—1925**



# POST-2000 PATENTED INVENTIONS

## LOW-VOLTAGE BALUN CIRCUIT



## 21 PREVIOUSLY PATENTED INVENTIONS REINVENTED BY GP

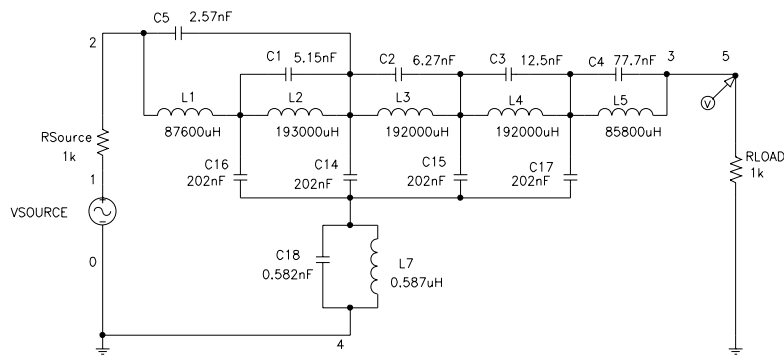
	<b>Invention</b>	<b>Date</b>	<b>Inventor</b>	<b>Place</b>	<b>Patent</b>
<b>1</b>	<b>Darlington emitter-follower section</b>	<b>1953</b>	<b>Sidney Darlington</b>	<b>Bell Telephone Laboratories</b>	<b>2,663,806</b>
<b>2</b>	<b>Ladder filter</b>	<b>1917</b>	<b>George Campbell</b>	<b>American Telephone and Telegraph</b>	<b>1,227,113</b>
<b>3</b>	<b>Crossover filter</b>	<b>1925</b>	<b>Otto Julius Zobel</b>	<b>American Telephone and Telegraph</b>	<b>1,538,964</b>
<b>4</b>	<b>“M-derived half section” filter</b>	<b>1925</b>	<b>Otto Julius Zobel</b>	<b>American Telephone and Telegraph</b>	<b>1,538,964</b>
<b>5</b>	<b>Cauer (elliptic) topology for filters</b>	<b>1934–1936</b>	<b>Wilhelm Cauer</b>	<b>University of Gottingen</b>	<b>1,958,742, 1,989,545</b>
<b>6</b>	<b>Sorting network</b>	<b>1962</b>	<b>Daniel G. O’Connor and Raymond J. Nelson</b>	<b>General Precision, Inc.</b>	<b>3,029,413</b>
<b>7</b>	<b>Computational circuits</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>
<b>8</b>	<b>Electronic thermometer</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>
<b>9</b>	<b>Voltage reference circuit</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>
<b>10</b>	<b>60 dB and 96 dB amplifiers</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>	<b>See text</b>
<b>11</b>	<b>Second-derivative controller</b>	<b>1942</b>	<b>Harry Jones</b>	<b>Brown Instrument Company</b>	<b>2,282,726</b>
<b>12</b>	<b>Philbrick circuit</b>	<b>1956</b>	<b>George Philbrick</b>	<b>George A. Philbrick Researches</b>	<b>2,730,679</b>
<b>13</b>	<b>NAND circuit</b>	<b>1971</b>	<b>David H. Chung and Bill H.</b>	<b>Texas Instruments Incorporated</b>	<b>3,560,760</b>

			<b>Terrell</b>		
<b>14</b>	<b>PID (proportional, integrative, and derivative) controller</b>	<b>1939</b>	<b>Albert Callender and Allan Stevenson</b>	<b>Imperial Chemical Limited</b>	<b>2,175,985</b>
<b>15</b>	<b>Negative feedback</b>	<b>1937</b>	<b>Harold S. Black</b>	<b>American Telephone and Telegraph</b>	<b>2,102,670, 2,102,671</b>
<b>16</b>	<b>Low-voltage balun circuit</b>	<b>2001</b>	<b>Sang Gug Lee</b>	<b>Information and Communications University</b>	<b>6,265,908</b>
<b>17</b>	<b>Mixed analog-digital variable capacitor circuit</b>	<b>2000</b>	<b>Turgut Sefket Aytur</b>	<b>Lucent Technologies Inc.</b>	<b>6,013,958</b>
<b>18</b>	<b>High-current load circuit</b>	<b>2001</b>	<b>Timothy Daun-Lindberg and Michael Miller</b>	<b>International Business Machines Corporation</b>	<b>6,211,726</b>
<b>19</b>	<b>Voltage-current conversion circuit</b>	<b>2000</b>	<b>Akira Ikeuchi and Naoshi Tokuda</b>	<b>Mitsumi Electric Co., Ltd.</b>	<b>6,166,529</b>
<b>20</b>	<b>Cubic function generator</b>	<b>2000</b>	<b>Stefano Cipriani and Anthony A. Takeshian</b>	<b>Conexant Systems, Inc.</b>	<b>6,160,427</b>
<b>21</b>	<b>Tunable integrated active filter</b>	<b>2001</b>	<b>Robert Irvine and Bernd Kolb</b>	<b>Infineon Technologies AG</b>	<b>6,225,859</b>

## **2 PATENTABLE INVENTIONS CREATED BY GENETIC PROGRAMMING**

	<b>Claimed invention</b>	<b>Date of patent application</b>	<b>Inventors</b>
<b>1</b>	<b>Improved general-purpose tuning rules for a PID controller</b>	<b>July 12, 2002</b>	<b>Martin A. Keane, John R. Koza, and Matthew J. Streeter</b>
<b>2</b>	<b>Improved general-purpose non-PID</b>	<b>July 12, 2002</b>	<b>Martin A. Keane, John R. Koza, and Matthew J. Streeter</b>

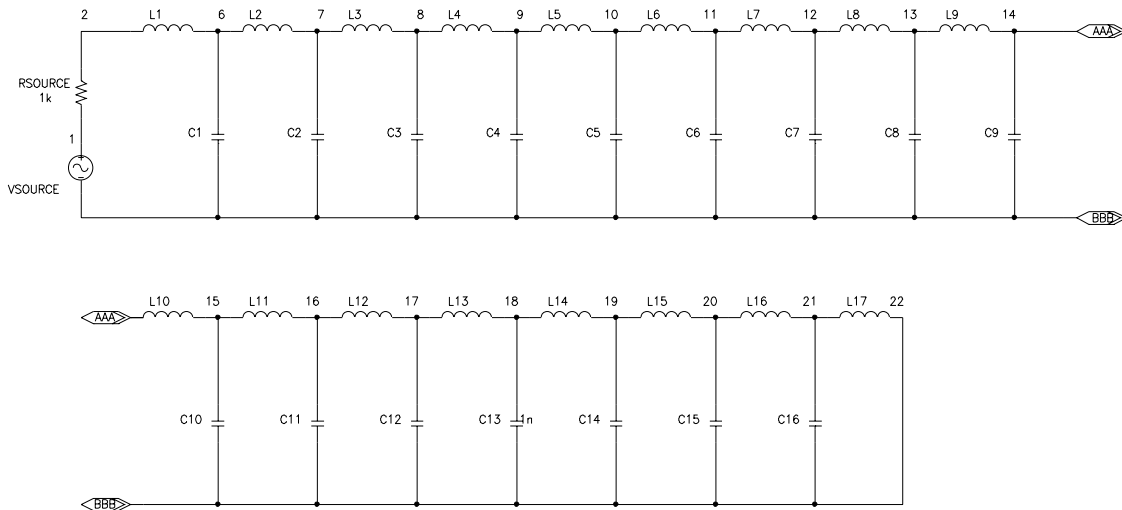
	<b>controllers</b>		
--	--------------------	--	--



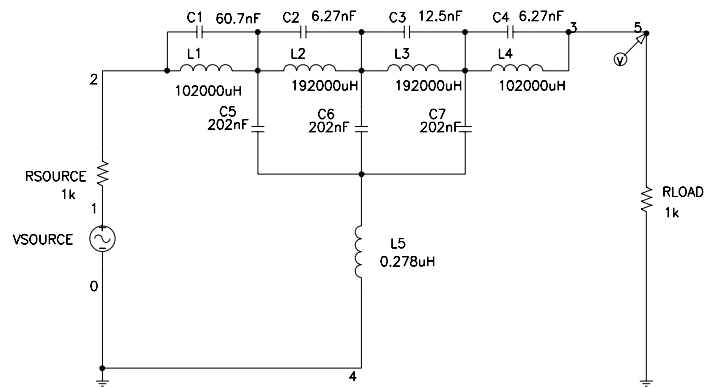
32

# NOVELTY-DRIVEN EVOLUTION

## PRIOR ART TEMPLATE



## SOLUTION NO. 1

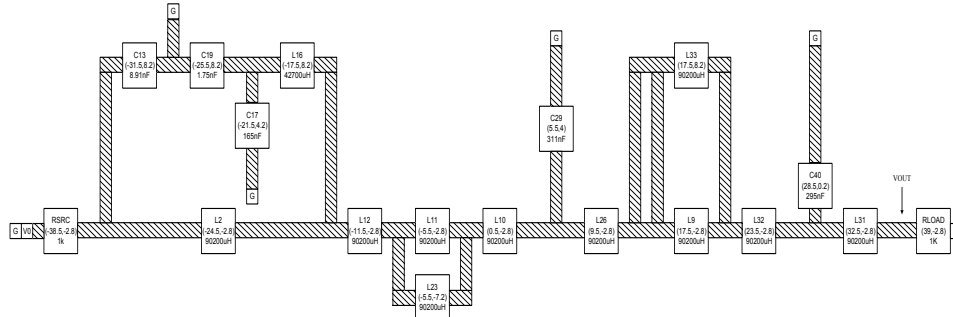


## SOLUTION NO. 5

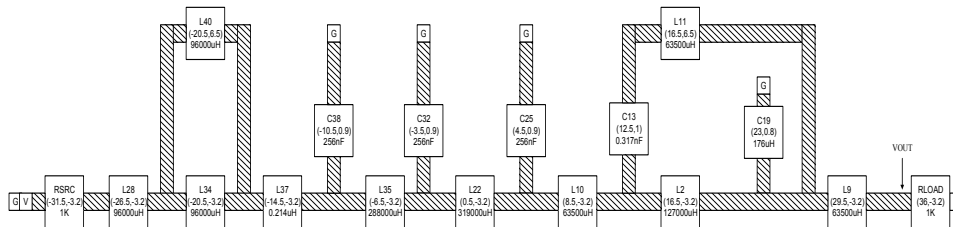


# LAYOUT — LOWPASS FILTER 100%-COMPLIANT CIRCUITS

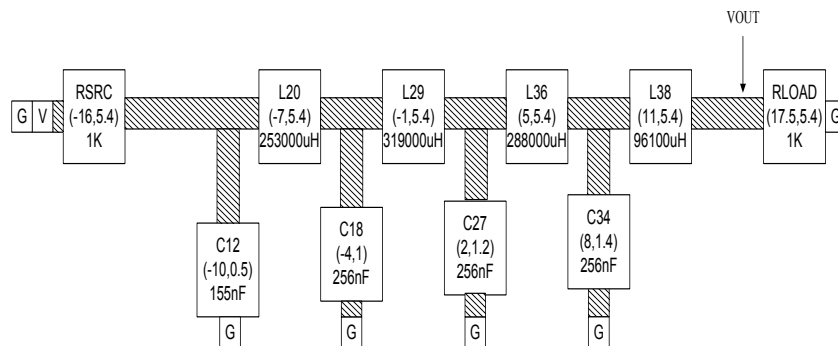
## GENERATION 25 WITH 5 CAPACITORS AND 11 INDUCTORS — AREA OF 1775.2



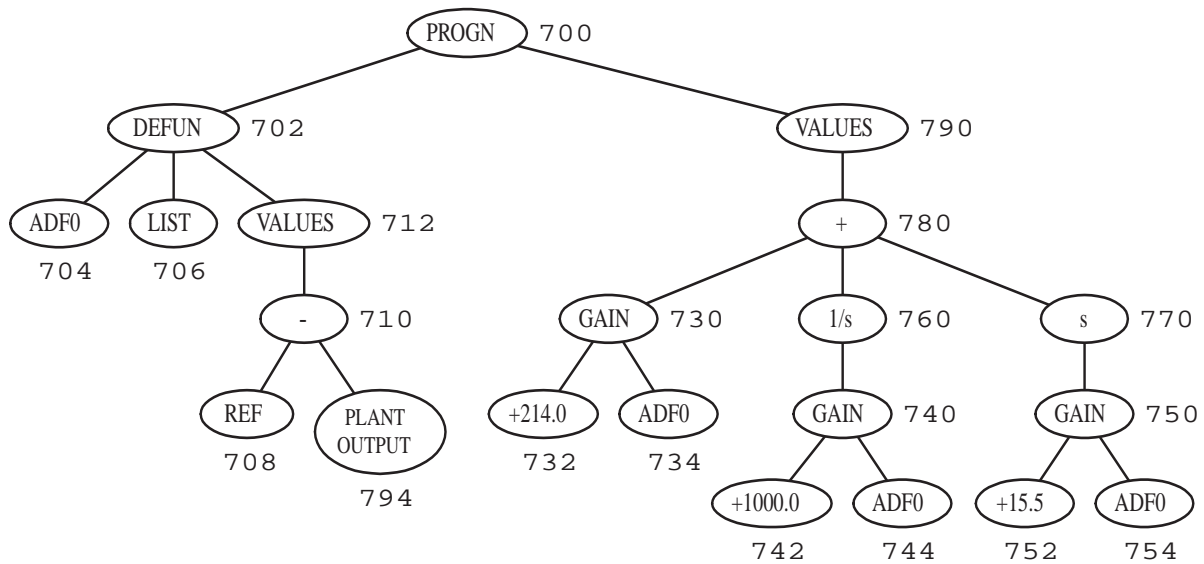
## GENERATION 30 WITH 10 INDUCTORS AND 5 CAPACITORS — AREA OF 950.3



## BEST-OF-RUN CIRCUIT OF GENERATION 138 WITH 4 INDUCTORS AND 4 CAPACITORS — AREA OF 359.4

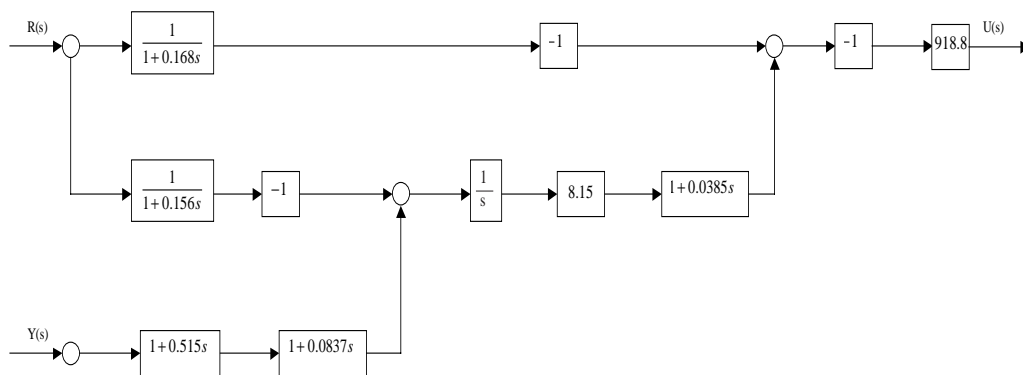


# CONTROLLERS



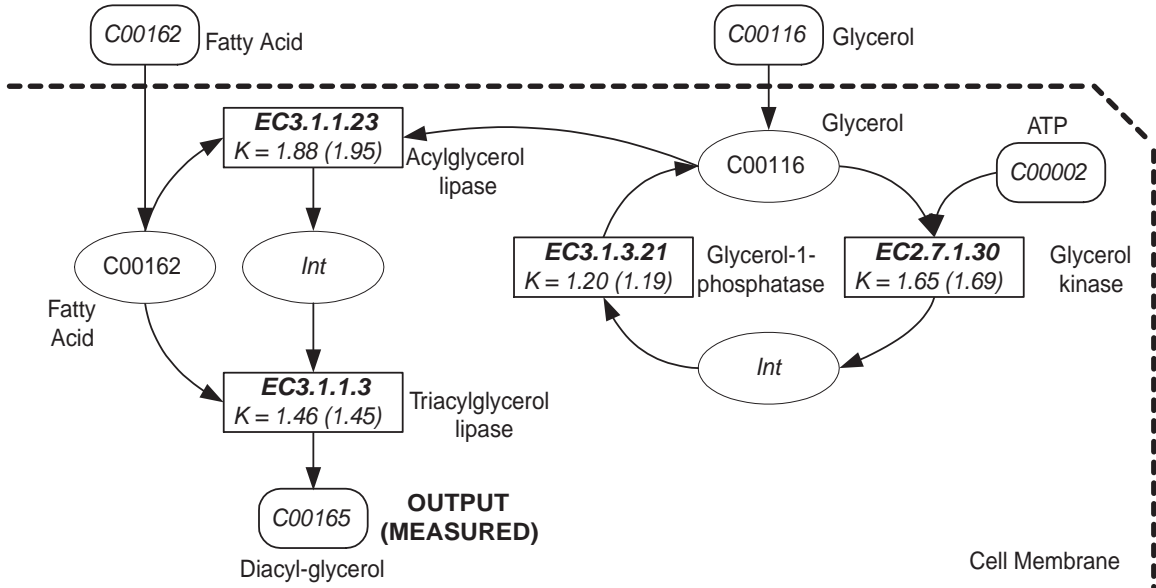
- **ADF can be used for internal feedback**

## BEST-OF-RUN GENETICALLY EVOLVED CONTROLLER FOR 2-LAG PLANT

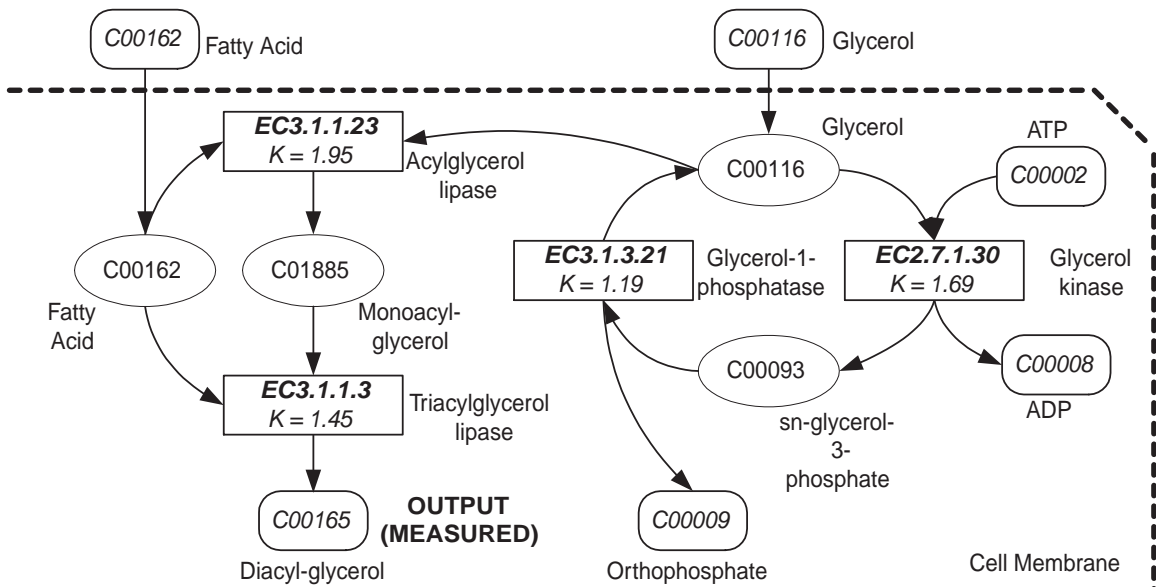


# REVERSE ENGINEERING OF METABOLIC PATHWAYS (4-REACTION NETWORK IN PHOSPHOLIPID CYCLE)

## BEST-OF-GENERATION 66



## DESIRED

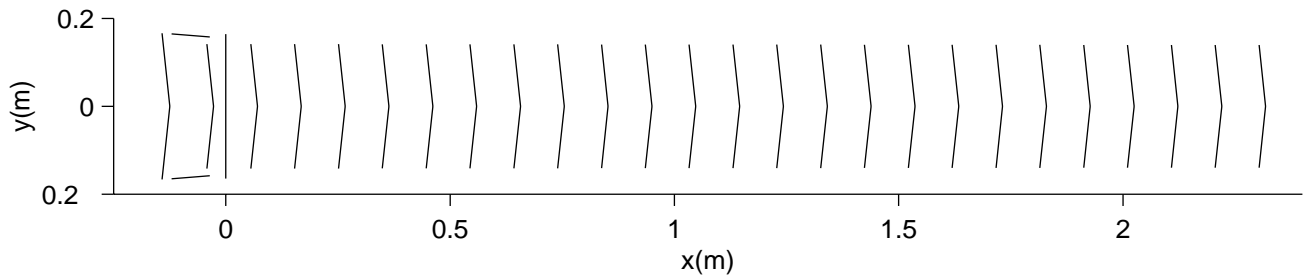
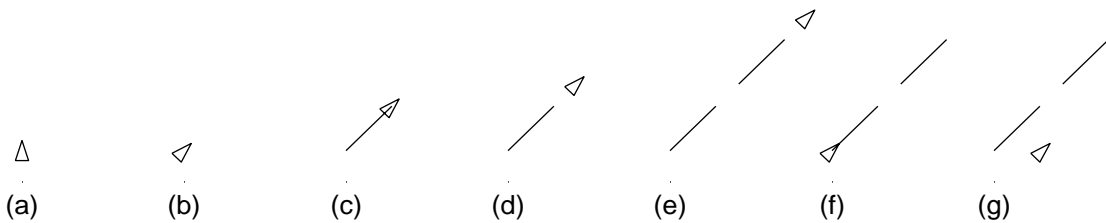


# AUTOMATIC SYNTHESIS OF ANTENNA

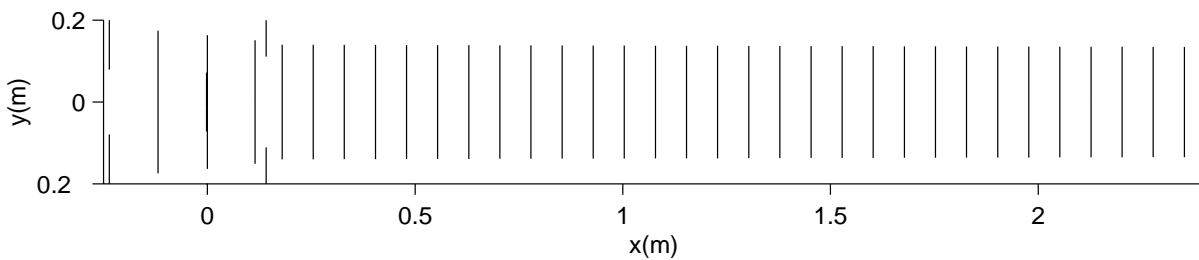
```

1 (PROGN3
2   (TURN-RIGHT 0.125)
3   (LANDMARK
4     (REPEAT 2
5       (PROGN2
6         (DRAW 1.0 HALF-MM-WIRE)
7         (DRAW 0.5 NO-WIRE)))
8   (TRANSLATE-RIGHT 0.125 0.75))

```



## BEST-OF-RUN ANTENNA



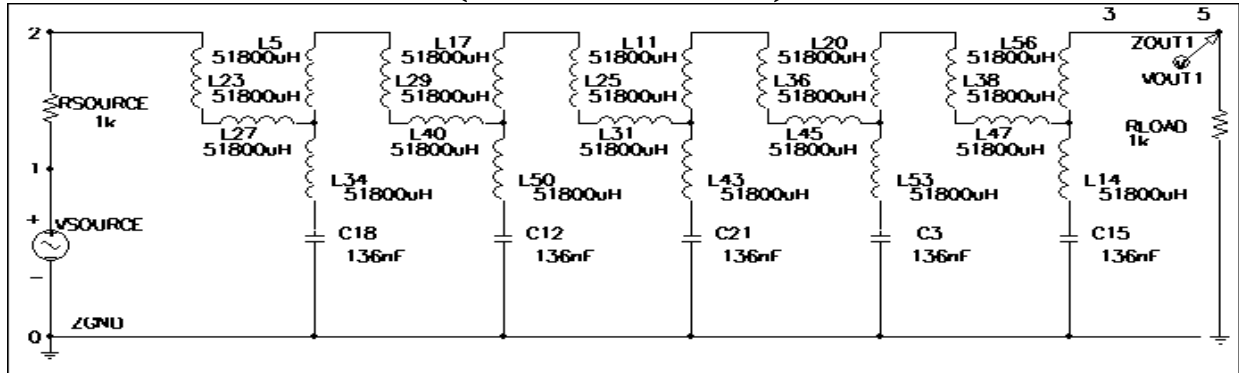
## **CHARACTERISTICS SUGGESTING THE USE OF GENETIC PROGRAMMING**

- (1) discovering the size and shape of the solution,**
- (2) reusing substructures,**
- (3) discovering the number of substructures,**
- (4) discovering the nature of the hierarchical references among substructures,**
- (5) passing parameters to a substructure,**
- (6) discovering the type of substructures (e.g., subroutines, iterations, loops, recursions, or storage),**
- (7) discovering the number of arguments possessed by a substructure,**
- (8) maintaining syntactic validity and locality by means of a developmental process, or**
- (9) discovering a general solution in the form of a parameterized topology containing free variables**

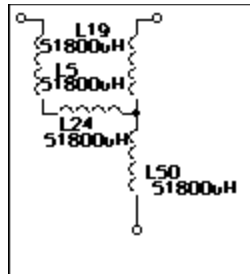
# REUSE

## LOWPASS FILTER USING ADFs

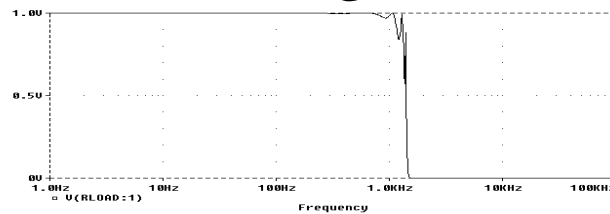
### GENERATION 31 — TOPOLOGY OF CAUER (ELLIPTIC) FILTER



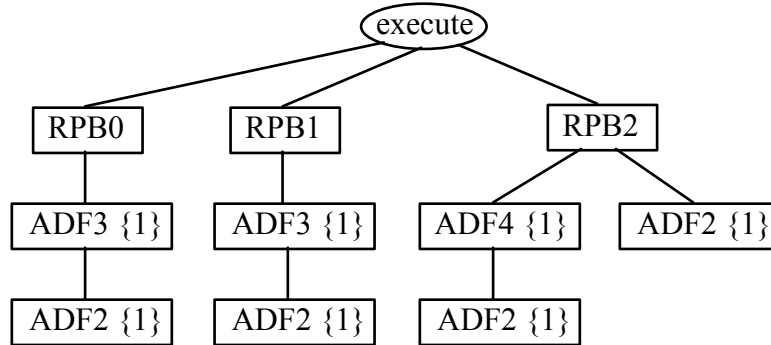
## QUINTUPLY-CALLED THREE-PORTED ADF0



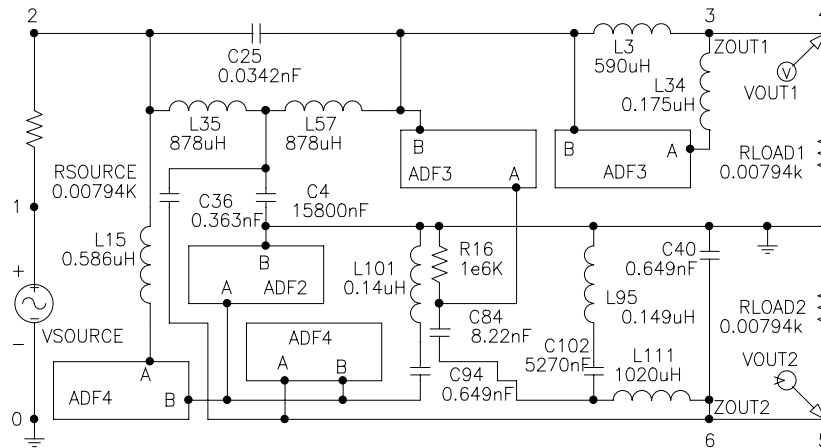
## BEHAVIOR IN FREQUENCY DOMAIN



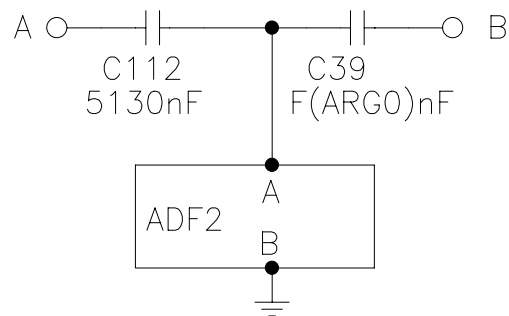
# PASSING A PARAMETER TO A SUBSTRUCTURE



## BEST-OF-RUN CIRCUIT

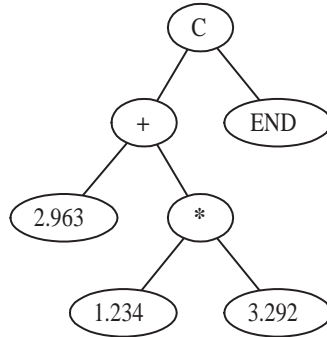


## THREE-PORTED ADF3

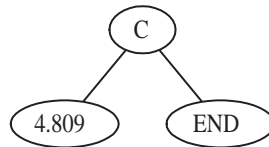


# VALUE-SETTING SUBTREES—3 WAYS

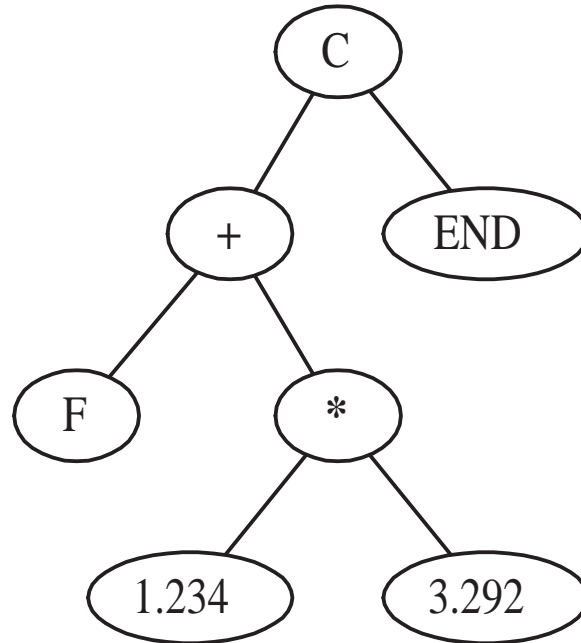
## ARITHMETIC-PERFORMING SUBTREE



## SINGLE PERTURBABLE CONSTANT



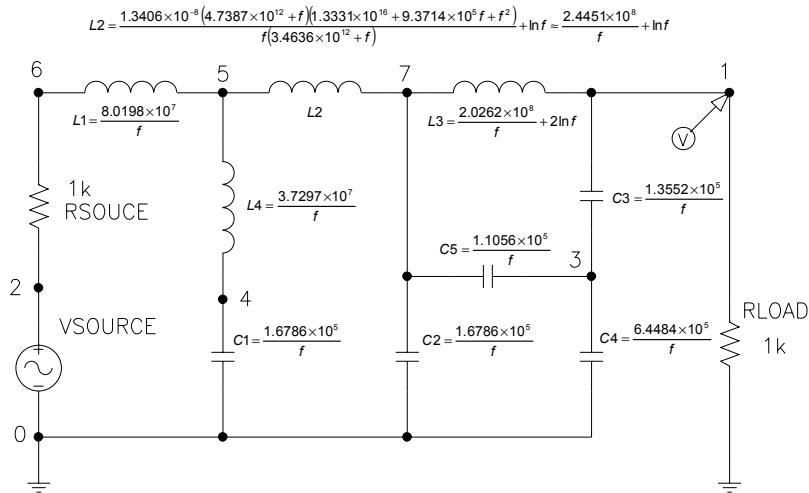
## FREE VARIABLE



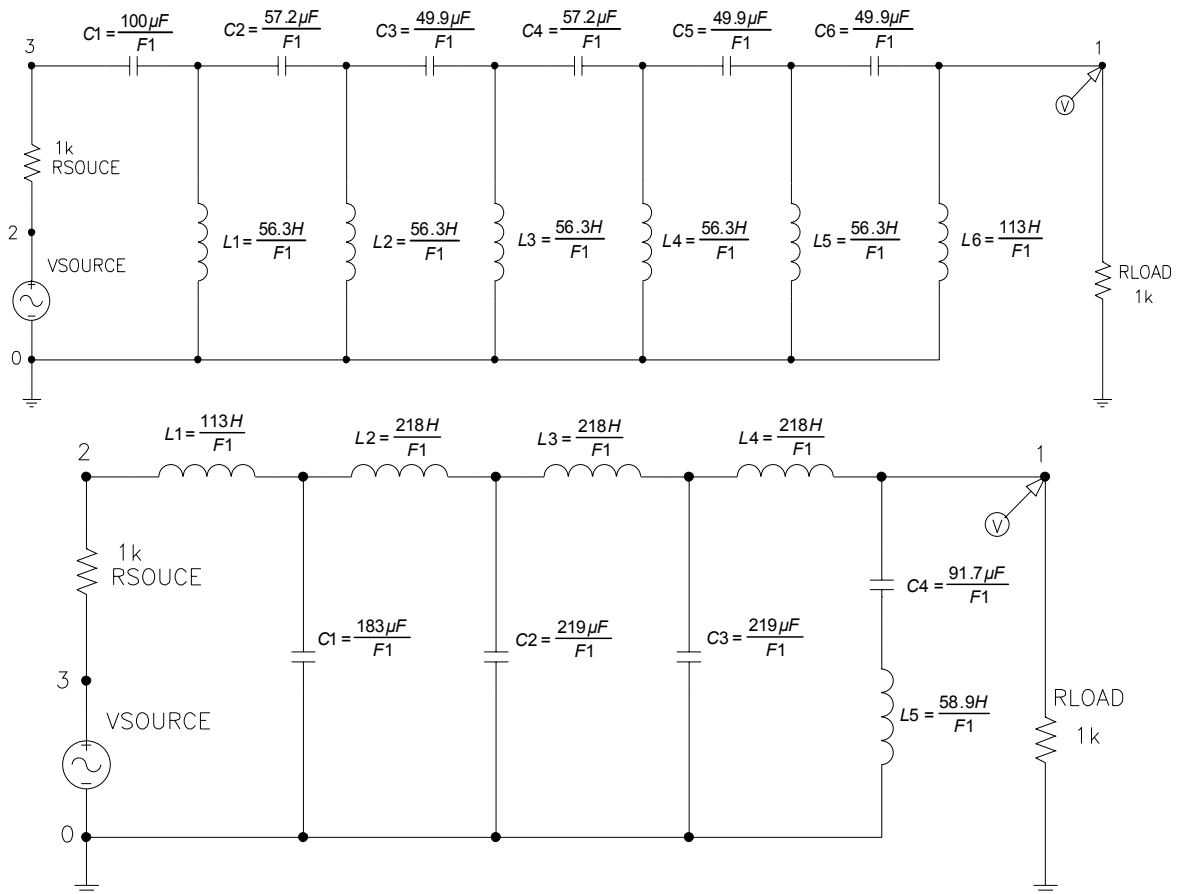


# PARAMETERIZED TOPOLOGIES (GIFS)

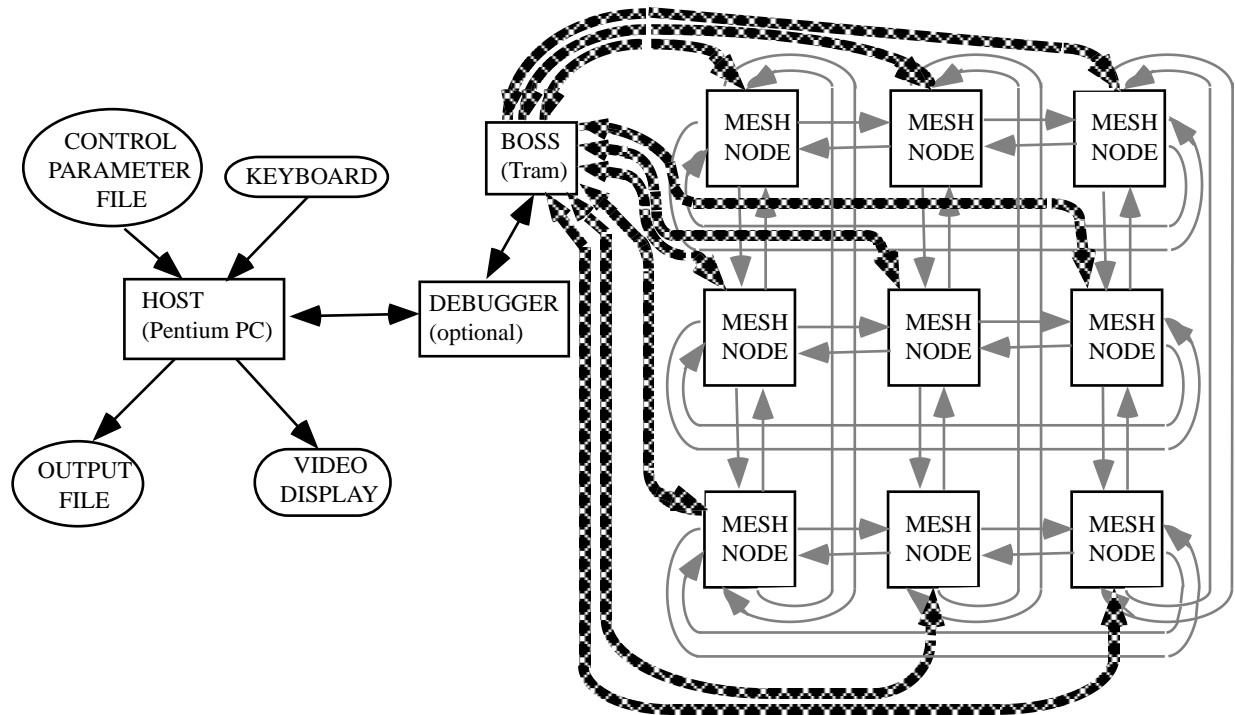
## VARIABLE CUTOFF LOWPASS FILTER



## LOWPASS/HIGHPASS FILTER



# PARALLELIZATION BY SUBPOPULATIONS ("ISLAND" OR "DEME" MODEL OR "DISTRIBUTED GENETIC ALGORITHM")



- Like Hormel, Get Everything Out of the Pig, Including the Oink
- Keep on Trucking
- It Takes a Licking and Keeps on Ticking
- The Whole is Greater than the Sum of the Parts

## PETA-OPS

- Human brain operates at  $10^{12}$  neurons operating at  $10^3$  per second =  $10^{15}$  ops per second
- $10^{15}$  ops = 1 peta-op = 1 bs (brain second)

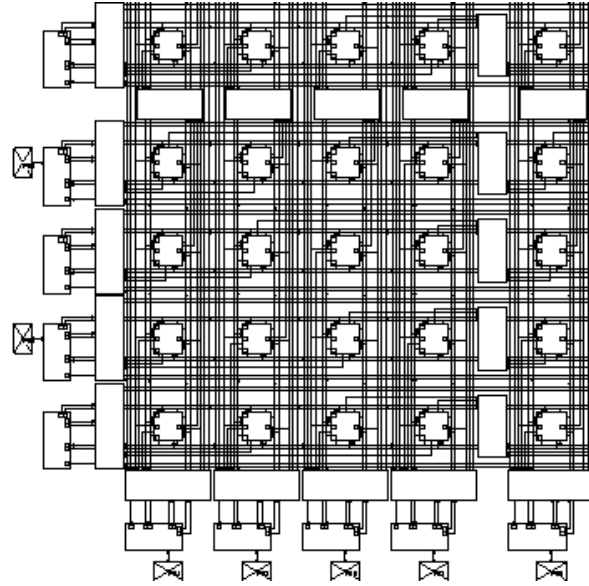
## GENETIC PROGRAMMING OVER 15- YEAR PERIOD 1987–2002

<b>System</b>	<b>Period of usage</b>	<b>Petacycles (10<sup>15</sup> cycles) per day for entire system</b>	<b>Speed-up over previous system</b>	<b>Speed-up over first system in this table</b>	<b>Human-competitive results</b>
<b>Serial Texas Instruments LISP machine</b>	<b>1987–1994</b>	<b>0.00216</b>	<b>1 (base)</b>	<b>1 (base)</b>	<b>0</b>
<b>64-node Transtech transputer parallel machine</b>	<b>1994–1997</b>	<b>0.02</b>	<b>9</b>	<b>9</b>	<b>2</b>
<b>64-node Parsytec parallel machine</b>	<b>1995–2000</b>	<b>0.44</b>	<b>22</b>	<b>204</b>	<b>12</b>
<b>70-node Alpha parallel machine</b>	<b>1999–2001</b>	<b>3.2</b>	<b>7.3</b>	<b>1,481</b>	<b>2</b>
<b>1,000-node Pentium II parallel machine</b>	<b>2000–2002</b>	<b>30.0</b>	<b>9.4</b>	<b>13,900</b>	<b>12</b>

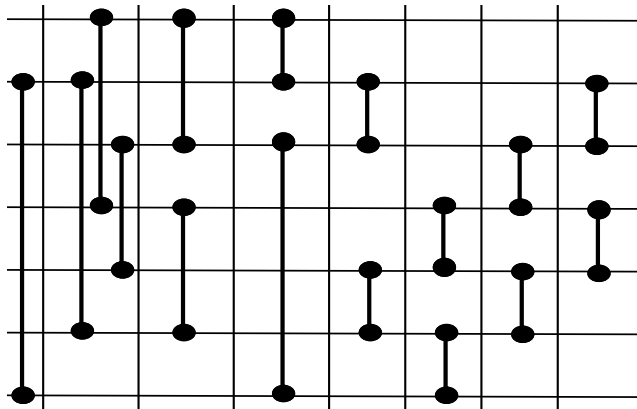
## PROGRESSION OF RESULTS

System	Period	Speed-up	Qualitative nature of the results produced by genetic programming
Serial LISP machine	1987–1994	1 (base)	<ul style="list-style-type: none"> <li>• Toy problems of the 1980s and early 1990s from the fields of artificial intelligence and machine learning</li> </ul>
64-node Transtech 8-biy transputer	1994–1997	9	<ul style="list-style-type: none"> <li>• Two human-competitive results involving one-dimensional discrete data (not patent-related)</li> </ul>
64-node Parsytec parallel machine	1995–2000	22	<ul style="list-style-type: none"> <li>• One human-competitive result involving two-dimensional discrete data</li> <li>• Numerous human-competitive results involving continuous signals analyzed in the frequency domain</li> <li>• Numerous human-competitive results involving 20<sup>th</sup>-century patented inventions</li> </ul>
70-node Alpha parallel machine	1999–2001	7.3	<ul style="list-style-type: none"> <li>• One human-competitive result involving continuous signals analyzed in the time domain</li> <li>• Circuit synthesis extended from topology and sizing to include routing and placement (layout)</li> </ul>
1,000-node Pentium II parallel machine	2000–2002	9.4	<ul style="list-style-type: none"> <li>• Numerous human-competitive results involving continuous signals analyzed in the time domain</li> <li>• Numerous general solutions to problems in the form of parameterized topologies</li> <li>• Six human-competitive results duplicating the functionality of 21<sup>st</sup>-century patented inventions</li> </ul>
Long (4-week) runs of 1,000-node Pentium II parallel machine	2002	9.3	<ul style="list-style-type: none"> <li>• Generation of two patentable new inventions</li> </ul>

# EVOLVABLE HARDWARE USING RAPIDLY RECONFIGURABLE FPGAs



# GENETICALLY EVOLVED 7-SORTER



# HUMAN-COMPETITIVENESS CRITERIA

	Criterion
A	The result was patented as an invention in the past, is an improvement over a patented invention, or would qualify today as a patentable new invention.
B	The result is equal to or better than a result that was accepted as a new scientific result at the time when it was published in a peer-reviewed scientific journal.
C	The result is equal to or better than a result that was placed into a database or archive of results maintained by an internationally recognized panel of scientific experts.
D	The result is publishable in its own right as a new scientific result—independent of the fact that the result was mechanically created.
E	The result is equal to or better than the most recent human-created solution to a long-standing problem for which there has been a succession of increasingly better human-created solutions.
F	The result is equal to or better than a result that was considered an achievement in its field at the time it was first discovered.
G	The result solves a problem of indisputable difficulty in its field.
H	The result holds its own or wins a regulated competition involving human contestants (in the form of either live human players or human-written computer programs).

## 37 HUMAN-COMPETITIVE RESULTS

	Claimed instance	Basis for claim of human-competitiveness	Reference
1	Creation of a better-than-classical quantum algorithm for the Deutsch-Jozsa “early promise” problem	B, F	Spector, Barnum, and Bernstein 1998
2	Creation of a better-than-classical quantum algorithm for Grover’s database search problem	B, F	Spector, Barnum, and Bernstein 1999
3	Creation of a quantum algorithm for the depth-two AND/OR query problem that is better than any previously published result	D	Spector, Barnum, Bernstein, and Swamy 1999; Barnum, Bernstein, and Spector 2000
4	Creation of a quantum algorithm for the depth-one OR query problem that is better than any previously published result	D	Barnum, Bernstein, and Spector 2000
5	Creation of a protocol for communicating information through a quantum gate that was previously thought not to permit such communication	D	Spector and Bernstein 2003
6	Creation of a novel variant of quantum dense coding	D	Spector and Bernstein 2003
7	Creation of a soccer-playing program that won its first two games in the Robo Cup 1997 competition	H	Luke 1998
8	Creation of a soccer-playing program that ranked in the middle of the field of 34 human-written programs in the Robo Cup 1998 competition	H	Andre and Teller 1999
9	Creation of four different algorithms for the transmembrane segment identification problem for proteins	B, E	Sections 18.8 and 18.10 of <i>GP-2 book</i> and sections 16.5 and 17.2 of <i>GP-3 book</i>
10	Creation of a sorting network for seven items using only 16 steps	A, D	Sections 21.4.4, 23.6, and 57.8.1 of <i>GP-3 book</i>

11	Rediscovery of the Campbell ladder topology for lowpass and highpass filters	A, F	Section 25.15.1 of GP-3 book and section 5.2 of GP-4 book
12	Rediscovery of the Zobel “ <i>M</i> -derived half section” and “constant <i>K</i> ” filter sections	A, F	Section 25.15.2 of GP-3 book
13	Rediscovery of the Cauer (elliptic) topology for filters	A, F	Section 27.3.7 of GP-3 book
14	Automatic decomposition of the problem of synthesizing a crossover filter	A, F	Section 32.3 of GP-3 book
15	Rediscovery of a recognizable voltage gain stage and a Darlington emitter-follower section of an amplifier and other circuits	A, F	Section 42.3 of GP-3 book
16	Synthesis of 60 and 96 decibel amplifiers	A, F	Section 45.3 of GP-3 book
17	Synthesis of analog computational circuits for squaring, cubing, square root, cube root, logarithm, and Gaussian functions	A, D, G	Section 47.5.3 of GP-3 book
18	Synthesis of a real-time analog circuit for time-optimal control of a robot	G	Section 48.3 of GP-3 book
19	Synthesis of an electronic thermometer	A, G	Section 49.3 of GP-3 book
20	Synthesis of a voltage reference circuit	A, G	Section 50.3 of GP-3 book
21	Creation of a cellular automata rule for the majority classification problem that is better than the Gacs-Kurdyumov-Levin (GKL) rule and all other known rules written by humans	D, E	Andre, Bennett, and Koza 1996 and section 58.4 of GP-3 book
22	Creation of motifs that detect the D–E–A–D box family of proteins and the manganese superoxide dismutase family	C	Section 59.8 of GP-3 book
23	Synthesis of topology for a PID-D2 (proportional, integrative, derivative, and second derivative) controller	A, F	Section 3.7 of GP-4 book
24	Synthesis of an analog circuit equivalent to Philbrick circuit	A, F	Section 4.3 of GP-4 book
25	Synthesis of a NAND circuit	A, F	Section 4.4 of GP-4 book
26	Simultaneous synthesis of topology, sizing, placement, and routing of analog electrical circuits	A, F, G	Chapter 5 of GP-4 book
27	Synthesis of topology for a PID (proportional, integrative, and derivative) controller	A, F	Section 9.2 of GP-4 book
28	Rediscovery of negative feedback	A, E, F, G	Chapter 14 of GP-4 book
29	Synthesis of a low-voltage balun circuit	A	Section 15.4.1 of GP-4 book
30	Synthesis of a mixed analog-digital variable capacitor circuit	A	Section 15.4.2 of GP-4 book
31	Synthesis of a high-current load circuit	A	Section 15.4.3 of GP-4 book
32	Synthesis of a voltage-current conversion circuit	A	Section 15.4.4 of GP-4 book
33	Synthesis of a Cubic function generator	A	Section 15.4.5 of GP-4 book
34	Synthesis of a tunable integrated active filter	A	Section 15.4.6 of GP-4 book
35	Creation of PID tuning rules that outperform the Ziegler-Nichols and Åström-Hägglund tuning rules	A, B, D, E, F, G	Chapter 12 of GP-4 book
36	Creation of three non-PID controllers that outperform a PID controller that use Ziegler-Nichols or Åström-Hägglund tuning rules	A, B, D, E, F, G	Chapter 13 of GP-4 book
37	Antenna for NASA Space Technology 5 Mission	B, D, E, G	Lohn, Hornby, Linden 2004

# PROMISING GP APPLICATION AREAS

- Problem areas involving many variables that are interrelated in highly non-linear ways
- Inter-relationship of variables is not well understood
- A good approximate solution is satisfactory
  - design
  - control
  - classification and pattern recognition
  - data mining
  - system identification and forecasting
- Discovery of the size and shape of the solution is a major part of the problem
- Areas where humans find it difficult to write programs
  - parallel computers
  - cellular automata
  - multi-agent strategies / distributed AI
  - FPGAs
- "black art" problems
  - synthesis of topology and sizing of analog circuits
  - synthesis of topology and tuning of controllers
  - quantum computing circuits
  - synthesis of designs for antennas
- Areas where you simply have no idea how to program a solution, but where the objective (fitness measure) is clear
- Problem areas where large computerized databases are accumulating and computerized techniques are needed to analyze the data



## **FUNDAMENTAL DIFFERENCES BETWEEN GP AND OTHER APPROACHES TO AI AND ML**

- (1) Representation: Genetic programming overtly conducts its search for a solution to the given problem in program space.**
- (2) Role of point-to-point transformations in the search: Genetic programming does not conduct its search by transforming a single point in the search space into another single point, but instead transforms a set of points into another set of points.**
- (3) Role of hill climbing in the search: Genetic programming does not rely exclusively on greedy hill climbing to conduct its search, but instead allocates a certain number of trials, in a principled way, to choices that are known to be inferior.**
- (4) Role of determinism in the search: Genetic programming conducts its search probabilistically.**
- (5) Role of an explicit knowledge base: None.**
- (6) Role of formal logic in the search: None.**
- (7) Underpinnings of the technique: Biologically inspired.**

# 17 AUTHORED BOOKS ON GP

- Banzhaf, Wolfgang, Nordin, Peter, Keller, Robert E., and Francone, Frank D. 1998. *Genetic Programming - An Introduction*. San Francisco, CA: [Morgan Kaufman Publishers](#) and Heidelberg, Germany: dpunkt.verlag.
- Babovic, Vladan. 1996b. *Emergence, Evolution, Intelligence: Hydroinformatics*. Rotterdam, The Netherlands: Balkema Publishers.
- Blickle, Tobias. 1997. *Theory of Evolutionary Algorithms and Application to System Synthesis*. TIK-Schriftenreihe Nr. 17. Zurich, Switzerland: [vdf Hochschul Verlag AG and der ETH Zurich](#). ISBN 3-7281-2433-8.
- Jacob, Christian. 1997. *Principia Evolvica: Simulierte Evolution mit Mathematica*. Heidelberg, Germany: dpunkt.verlag. In German. English translation forthcoming in 2000 from [Morgan Kaufman Publishers](#).
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- Koza, John R. 1992. [Genetic Programming: On the Programming of Computers by Means of Natural Selection](#). Cambridge, MA: The MIT Press.
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- Koza, John R., Bennett III, Forrest H, Andre, David, and Keane, Martin A. 1999a. [Genetic Programming III: Darwinian Invention and Problem Solving](#). San Francisco, CA: Morgan Kaufmann Publishers.
- Koza, John R., Keane, Martin A., Streeter, Matthew J., Mydlowec, William, Yu, Jessen, and Lanza, Guido. 2003. *Genetic Programming IV. Routine Human-Competitive Machine Intelligence*. Kluwer Academic Publishers.
- Langdon, William B. 1998. [Genetic Programming and Data Structures: Genetic Programming + Data Structures = Automatic Programming!](#) Amsterdam: Kluwer Academic Publishers.
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- O'Neill, Michael and Ryan, Conor. 2003. *Grammatical Evolution: Evolutionary Automatic Programming in an Arbitrary Language*. Boston: Kluwer Academic Publishers.
- Ryan, Conor. 1999. *Automatic Re-engineering of Software Using Genetic Programming*. Amsterdam: Kluwer Academic Publishers.
- Spector, Lee. 2004. *Automatic Quantum Computer Programming: A Genetic Programming Approach*. Boston: Kluwer Academic Publishers.
- Wong, Man Leung and Leung, Kwong Sak. 2000. *Data Mining Using Grammar Based Genetic Programming and Applications*. Amsterdam: Kluwer Academic Publishers.

# SOME RECENT CONFERENCE PROCEEDINGS

- Banzhaf, Wolfgang, Daida, Jason, Eiben, A. E., Garzon, Max H., Honavar, Vasant, Jakiela, Mark, and Smith, Robert E. (editors). 1999. *GECCO-99: Proceedings of the Genetic and Evolutionary Computation Conference, July 13-17, 1999, Orlando, Florida USA*. San Francisco, CA: Morgan Kaufmann.
- Banzhaf, Wolfgang, Poli, Riccardo, Schoenauer, Marc, and Fogarty, Terence C. 1998. *Genetic Programming: First European Workshop. EuroGP'98. Paris, France*. Lecture Notes in Computer Science. Volume 1391. Berlin, Germany: Springer-Verlag.
- Koza, John R., Goldberg, David E., Fogel, David B., and Riolo, Rick L. (editors). 1996.  
Genetic Programming 1996: Proceedings of the First Annual Conference. Cambridge, MA: The MIT Press.
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