Automatic Synthesis of Both the Topology and Tuning of a Common Parameterized Controller for Two Families of Plants using Genetic Programming

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Abstract

This paper demonstrates that genetic programming can be used to automatically create the design for both the topology and parameter values (tuning) for a common parameterized controller for all the plants in two families of plants that are representative of typical industrial processes. The genetically evolved controller is "general" in the sense that it contains free variables representing the characteristics of the particular plant. The genetically evolved controller outperforms the controller designed with conventional techniques. In addition, the genetically evolved controller infringes on an early patented invention in the field of control.

1 Introduction

Automatic controllers are ubiquitous in the real world. The purpose of a controller is to force, in a meritorious way, the actual response of a system (conventionally called the *plant*) to match a desired response (the *reference signal* or *setpoint*). For example, the cruise control device in a car continuously adjusts the engine (the plant) based on the difference between the speed specified by the driver (the *reference signal*) and the car's actual speed (the *plant response*).

Genetic programming has recently been used to automatically create the design for both the topology and parameter values (tuning) for a controller for a particular two-lag plant and a particular three-lag plant (Koza, Keane, Yu, Bennett, and Mydlowec 2000). However, these two (different) evolved controllers applied only to particular plants (of the same family).

The question arises as to whether it is possible to evolve a common controller (accessing various parameters representing the overall characteristics of the plant) that can perform well for an entire family of plants (say, the n-lag plants) and perhaps also for one or more additional families of plants.

In their influential book, Astrom and Hagglund (1995) identified four families of plants "that are representative for the dynamics of typical industrial processes." Astrom and Hagglund then developed a common method for designing controllers and demonstrated improved performance for their method over the Ziegler-Nichols (1942) rules on all the plants in all four families of plants.

One of the four families consists of the n-lag plants represented by transfer functions of the form

$$G(s) = \frac{1}{(1+s)^n} \qquad (1)$$

where n = 3, 4, and 8 and where s is the Laplace transform variable.

Another family consists of plants represented by

$$G(s) = \frac{1}{(1+s)(1+\alpha s)(1+\alpha^2 s)(1+\alpha^3 s)} \qquad (2)$$

where α = 0.2, 0.5, and 0.7.

The methods developed by Astrom and Hagglund use pairs of parameters representing the overall characteristics of a plant. These parameters are not, of course, a complete representation of the behavior of the plant; however, they offer the practical advantage of usually being obtainable for a given plant by means of relatively straight-forward testing in the field.

In one of their methods, Astrom and Hagglund use two frequency domain parameters, namely the ultimate gain, K_u (the minimum value of the gain that must be introduced into the feedback path to cause a system to oscillate) and the ultimate period, T_u (the period of this lowest frequency oscillation).

In another version, Astrom and Hagglund use the time constant, T_r, and the dead time, L. Astrom and Hagglund describe a procedure for estimating these two parameters from the plant's response to a step input. These two parameters are obtained by approximating the plant with the transfer function

$$\frac{e^{-sL}}{(1+sT_r)^2}$$

This paper shows that genetic programming can be used to automatically create the design for both the topology and tuning for a common parameterized controller for all plants belonging to the two families of plants described by equations (1) and (2). The common parameterized controller is created using a fitness measure that optimizes step response and disturbance rejection, while simultaneously constraining maximum sensitivity and sensor noise attenuation. The common genetically evolved controller outperforms the controller designed using the techniques of Astrom and Hagglund 1995.

Section 2 discusses how genetic programming can be used to automatically synthesize the design for both the topology and tuning of controllers. Section 3 itemizes the preparatory steps necessary to apply genetic programming to the above two families of plants. Section 4 presents the results.

2 Genetic Programming and Control

In a closed-loop continuous-time feedback system consisting of a plant and its controller, the output of the controller is input to the plant and the output of the plant is, in turn, input to the controller.

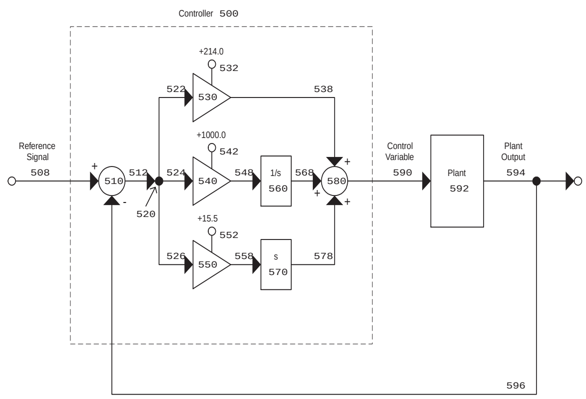

Figure 1 Block diagram of a plant and a PID controller composed of proportional, integrative, and derivative blocks.

Figure 1 is a block diagram for an illustrative control system containing a controller and a plant. The directed lines in a block diagram represent time-domain signals while the blocks represent signal processing functions that operate in the time domain. The output of the controller 500 is a control variable 590 which is, in turn, the input to the plant 592. The plant has one output (plant response) 594. The plant response is fed back (externally as signal 596) and becomes one of the controller's two inputs. The controller's second input is the reference signal 508. The fed-back plant response 596 and the externally supplied reference signal 508 are compared (by subtraction here). Notice that the takeoff point 520 of figure 1 provides a way to disseminate a particular result (of the subtraction 510) to three places in the block diagram (522, 524, and 526). The output (i.e., control variable 590) of this controller is the sum of three terms. First, there is a proportional (P) term (the gain block 530 with an amplification factor of 214.0). Second, there is an integrating (I) term (the integrator 560 preceded by the gain block 540 with an amplification factor of 1,000.0). The integrator is shown in the figure as 1/*s*. Third, there is a a differentiating (D) term (the derivative block 570 preceded by the gain block 550 with an amplification factor of 15.5). The derivative is shown in the figure as *s*. Since the controller's output is the sum of a P, I, and D term, this type of controller is called a PID controller. The PID controller was invented and patented by Albert Callender and Allan Stevenson of Imperial Chemical Limited of Northwich, England (Callender and Stevenson 1939).

Genetic programming (Koza 1992; Koza and Rice 1992; Koza 1994a, 1994b; Koza, Bennett, Andre, and Keane 1999; Koza, Bennett, Andre, Keane, and Brave 1999) is an extension of the genetic algorithm (Holland 1975). Additional information on genetic programming can be found in books such as Banzhaf, Nordin, Keller, and Francone 1998; books such as Langdon 1998, Ryan 1999, and Wong and Leung 2000 in the series on genetic programming from Kluwer Academic Publishers; in edited collections of papers such as the *Advances in Genetic Programming* series of books from the MIT Press (Spector, Langdon, O'Reilly, and Angeline 1999); in the proceedings of the Genetic Programming Conference (Koza, Banzhaf, Chellapilla, Deb, Dorigo, Fogel, Garzon, Goldberg, Iba, and Riolo 1998); in the proceedings of the Euro-GP conference (Poli, Nordin, Langdon, and Fogarty 1999); in the proceedings of the Genetic and Evolutionary Computation Conference (Banzhaf, Daida, Eiben, Garzon, Honavar, Jakiela, and Smith 1999); at web sites such as `www.genetic-programming.org`; and in the *Genetic Programming and Evolvable Machines* journal (from Kluwer Academic Publishers).

Evolutionary computation has been previously used for synthesizing controllers having mutually interacting continuous-time signal processing blocks and for system identification problems (Marenbach, Bettenhausen, and Freyer 1996). (Extensive references are itemized in Koza, Keane, Yu, Bennett, and Mydlowec 2000.)

There are several different styles that are commonly used in genetic programming. As one example, genetic programming is often used as an automatic method for creating a program tree to solve a problem (Koza 1992). The individual programs that are evolved by genetic programming are typically multi-branch programs consisting of result-producing branches, automatically defined functions (subroutines), and other types of branches. In this approach, the program tree is simply executed. The result of the execution may be a set of returned values, a set of side effects on some other entity (e.g., an external entity such as a robot or an internal entity such as computer memory), or a combination of returned values and side effects. In this approach, the functions in the program are sequentially executed, in time, in accordance with a specified "order of evaluation" such that the result of executing one function is available at the time when the next function is to be executed. Early work on the problem of automatically creating controllers used this conventional approach to genetic programming.

As a second example, genetic programming is often also used to automatically create program trees which can be used in conjunction with a developmental process to design complex structures, such as neural networks (Gruau 1992) and analog electrical circuits (Koza, Bennett, Andre, and Keane 1996; Koza, Bennett, Andre, and Keane 1999). In this approach, the program tree is interpreted as a set of instructions for constructing the desired structure. The construction process is implemented by applying the functions of a program tree to an embryonic structure so as to develop the embryo into a fully developed structure. As in the first approach, the functions of the program are executed separately, in time, in accordance with the specified "order of evaluation."

In this paper, a computer program (i.e., program tree, LISP symbolic expression) will represent the block diagram of a controller. The block diagram consists of signal processing functions linked by directed lines representing the flow of information. There is no "order of evaluation" of the functions and terminals of a program tree representing a controller. Instead, the signal processing blocks of the controller and the to-be-controlled plant interact with one another other as part of a closed system in the manner specified by the topology of the block diagram.

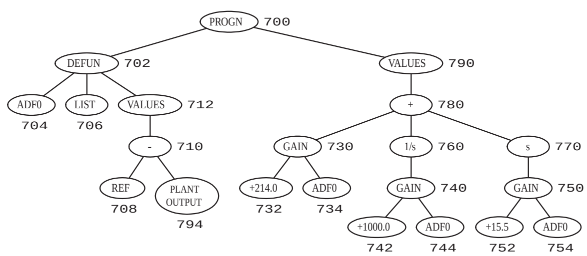

Figure 2 Program tree representation of the PID controller of figure 1.

Figure 2 presents the block diagram for the PID controller of figure 1 as a program tree. The internal points of this program tree represent the signal processing blocks contained in the block diagram of figure 1 (i.e., derivative, integrator, gain, subtraction, addition). The external points (leaves) of this program tree represent numerical constants and time-domain signals, such as the reference signal and plant output. Notice that automatically defined function (subroutine) ADF0 in the left branch produces a time-domain signal that equals the result of subtracting the plant output from the reference signal. The three references to ADF0 in the result-producing (right) branch of this program tree disseminate the result of subtracting the plant output from the reference signal and correspond to the takeoff point 520 of figure 1.

In the style of ordinary computer programming, a reference to a subroutine ADF0 from inside ADF0 would be considered to be a recursive reference. However, in the context of genetic programming and control systems, a subroutine that references itself corresponds to a loop in the controller's block diagram (i.e., internal feedback inside the controller).

3 Preparatory Steps

3.1 Program Architecture

Since the to-be-synthesized controller has one output (control variable), each program tree in the population has one result-producing branch. Each program tree in the initial random population (generation 0) has no automatically defined functions. However, after generation 0, the architecture-altering operations may insert (and delete) automatically defined functions. Automatically defined functions may be used for takeoff points, internal feedback within the controller, and reuse of portions of the block diagram. The permitted maximum of five automatically defined functions is more than sufficient for this problem.

3.2 Terminal Set

The numerical parameter value for each signal processing block possessing a parameter is established by an arithmetic-performing subtree containing perturbable numerical terminals, arithmetic operations, and the four parameters for representing the overall characteristics of a plant. Arithmetic-performing subtrees may appear in both result-producing branches and any automatically defined functions that may be created during the run by the architecture-altering operations. The value returned by an entire arithmetic-performing subtree is interpreted as a component value lying in a range of (positive values) between 10^{-3} and 10^{3}. The terminal set for the arithmetic-performing subtrees is

$T_{aps} = \{\Re, KU, TU, L, TR\}$.

Here $\Re$ denotes a perturbable numerical value. In the initial random generation (generation 0) of a run, each perturbable numerical value is set, individually and separately, to a random value in a chosen range (from -3.0 and +3.0 here). In later generations, a perturbable numerical value may be changed by adding or subtracting a relatively small number determined probabilistically by a Gaussian probability distribution. The standard deviation of the Gaussian distribution is 1.0 here (i.e., one order of magnitude after the value returned by an entire arithmetic-performing subtree is interpreted). The perturbations are implemented by a genetic operation for mutating the perturbable numerical values. The perturbable numerical values are coded by 30 bits in our system. A constrained syntactic structure maintains one function and terminal set for the arithmetic-performing subtrees and a different function and terminal set (below) for all other parts of the program tree.

The remaining terminals are time-domain signals. The terminal set, T, for the result-producing branch and any automatically defined functions (except the arithmetic-performing subtrees described above) is

T = {REFERENCE_SIGNAL,
CONTROLLER_OUTPUT, PLANT_OUTPUT}.

Space does not permit a detailed description of the various terminals used herein (although the meaning of the above terminals should be clear from their names). See Koza, Keane, Yu, Bennett, and Mydlowec 2000.

3.3 Function Set

The function set, F_{aps}, for the arithmetic-performing subtrees is

F_{aps} = {ADD_NUMERIC, SUB_NUMERIC,
MUL_NUMERIC, DIV_NUMERIC, REXP,
RLOG}.

The two-argument DIV_NUMERIC function divides the first argument by the second argument, except that the quotient is never allowed to exceed 10^5. The one-argument REXP function is the exponential function and the one-argument RLOG function is the natural logarithm of the absolute value.

The function set, F, for the result-producing branch and any automatically defined functions (except the arithmetic-performing subtrees described above) consists of continuous-time signal processing functions and automatically defined functions.

F = {GAIN, INVERTER, LEAD, LAG, LAG2,
DIFFERENTIAL_INPUT_INTEGRATOR,
DIFFERENTIATOR, ADD_SIGNAL,
SUB_SIGNAL, ADD_3_SIGNAL,
MUL_SIGNAL, DIV_SIGNAL, ULIMIT,
ADF0, ADF1, ADF2, ADF3, ADF4}.

The one-argument ULIMIT function limits a signal by constraining it between an upper and lower bound. This function returns the value of its argument (the incoming signal) when its argument lies between -1.0 and +1.0. If the argument is greater than +1.0, the function returns +1.0. If the argument is less than -1.0, the function returns -1.0. ADF0, …, ADF4 denote automatically defined functions added during the run by the architecture-altering operations. The definitions of the other functions above are suggested by their names. See Koza, Keane, Yu, Bennett, and Mydlowec 2000.

3.4 Fitness Measure

Genetic programming is a probabilistic algorithm that searches the space of compositions of the available functions and terminals under the guidance of a fitness measure. The fitness measure is a mathematical implementation of the problem's high-level requirements. It is couched in terms of "what needs to be done" — not "how to do it." The fitness measure for most problems of controller design is multi-objective in the sense that there are several different (usually conflicting) requirements for the controller.

The fitness of each individual in the population is determined by executing the program tree (i.e., the result-producing branch plus any automatically defined functions that may have been created during the run by the architecture-altering operations). The execution of the program tree produces an interconnected sequence of signal processing blocks — that is, a block diagram for the individual controller. The controller is embedded into a framework containing the (fixed) plant and the (fixed) external feedback loop. A SPICE netlist is then constructed to represent the block diagram of the controller, the (fixed) plant, and the (fixed) external feedback loop. This SPICE netlist is wrapped inside an appropriate set of SPICE commands to carry out various SPICE analyses in the time domain (described below). We also provide SPICE with subcircuit definitions to implement all the signal processing functions in the function set (described above) and all the signal processing functions necessary to represent the plant. The controller is then simulated using our modified version of the original 217,000-line SPICE3 simulator (Quarles, Newton, Pederson, and Sangiovanni-Vincentelli 1994). Our modified version of SPICE is run as a submodule within our genetic programming system. The SPICE simulator returns tabular output (representing the plant output in the time domain). An interface communicates this information to our genetic programming code. See Koza, Keane, Yu, Bennett, and Mydlowec 2000 for details.

The fitness of each controller in the population is measured by means of 48 separate invocations of the SPICE simulator. This 48-part fitness measure attempts to optimize step response and disturbance rejection while simultaneously imposing constraints on maximum sensitivity and sensor noise attenuation. The fitness of an individual controller is the sum of the detrimental contributions of these 48 elements of the fitness measure. The smaller the sum, the better.

The first 36 elements of this 48-part fitness measure are time-domain-based elements that together represent the six plants from the two families (i.e., n = 3, 4, and 8 and α = 0.2, 0.5, and 0.7), in conjunction with six choices of values for the height of the reference signal and disturbance signal (shown in table 1) that sample a range of values. The reference signal is step function that rises from 0 at time $t = 0$ to the specified height at t = 1 millisecond. The disturbance signal is a step function that rises from 0 at time $t = 10T_u$ to the specified height at $t = 10T_u + 1$ millisecond. The disturbance signal is added to the controller's output.

Table 1 Six combinations

Reference signal	Disturbance signal
1.0	1.0
10^{-3}	10^{-3}

-10^{-6}	10^{-6}
1.0	-0.6
-1.0	0.0
0.0	1.0

For each of these first 36 elements of the 48-part fitness measure, a transient analysis is performed in the time domain using the SPICE simulator. $e(t)$ is the difference (error) at time t between the plant output and the reference signal. The contribution to fitness for each of these 36 elements is based on the sum of two integrals of time-weighted absolute error (ITAE). The first term of the integral accounts for the controller's step response while the second term accounts for disturbance rejection.

$$\frac{\int_{t=0}^{10T_u} t\left|e(t)\right|Bdt}{T_u^2}+\frac{\int_{t=10T_u}^{20T_u} (t-10T_u)\left|e(t)\right|Cdt}{T_u^2}.$$

The factor B in the first term of the integral multiplies each value of $e(t)$ by the reciprocal of the amplitude of the reference signal (so that all reference signals are equally influential). The factor C in the second term of the integral multiplies value of $e(t)$ by the reciprocal of the amplitude of the disturbance signals. When the amplitude of either the reference signal or the disturbance signal is zero, the appropriate factor (B or C) is set to zero. The ITAE component of fitness is such that, all other things being equal, changing the time scale by a factor of F changes the ITAE by F^2. The division of the integral by T_u^2 is an attempt to eliminate this artifact of the time scale and equalize the influence of each of the plants in the overall fitness measure. For these 36 elements of the fitness measure, the contribution to fitness is multiplied by 20 if the element is greater than for the Astrom and Hagglund (1995).

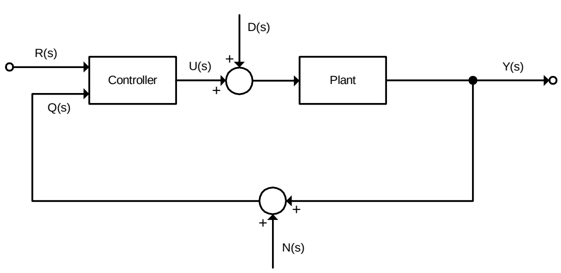

Figure 3 Overall model.

The 37th through 42nd elements of the 48-part fitness measure are frequency-domain-based elements that measure stability margin. Figure 3 presents a model for the entire system containing the given plant and the to-be-evolved controller. In this figure, $R(s)$ is the reference signal; $Y(s)$ is the plant output; and $U(s)$ is the controller's output (control variable). Disturbance $D(s)$ may be added to the controller's output $U(s)$. Sensor noise $N(s)$ may be added to the plant's output $Y(s)$ yielding $Q(s)$. Here $N(s)$ is an AC signal. For each of these six elements of the fitness measure, an AC sweep is performed using the SPICE simulator from $1/(1000T_u)$ to $1000/T_u$ while holding the reference signal $R(s)$ and the disturbance signal $D(s)$ at zero. The maximum sensitivity, M_s, is a measure of the stability margin. It is desirable to minimize the maximum sensitivity (and therefore maximize the stability margin). The quantity $1/M_s$ is the minimum distance between the Nyquist plot and the point (-1,0) and is the stability margin incorporating both gain and phase margin. The maximum sensitivity is the maximum amplitude of $Q(s)$. The contribution to fitness is 0 if $M_s < 1.5$; $2(M_s - 1.5)$ for $1.5 \le M_s \le 2.0$; and $20(M_s - 2.0) + 1$ for $M_s > 2.0$. For these six elements of the fitness measure (as well as the six elements below), the contribution to fitness is multiplied by 10 if the element is greater than for the Astrom and Hagglund controller (1995).

The 43rd through 48th elements of this 48-part fitness measure are frequency-domain-based elements measuring the sensor noise attenuation. Achieving favorable sensor noise attenuation is often in direct conflict with the goal of achieving a rapid response to setpoint changes and rejection of plant disturbances. For each of these six elements of the fitness measure, an AC sweep is performed using the SPICE simulator from $10/T_u$ to $1000/T_u$ while holding the reference signal $R(s)$ and the disturbance signal; $D(s)$ at zero. The attenuation of the sensor noise is measured at plant output at $Y(s)$. A_{min} is the minimum attenuation in decibels within this frequency range. It is desirable to maximize the minimum attenuation. The contribution to fitness for sensor noise attenuation is 0 if $A_{min} > 40$ dB; $(40 - A_{min})/10$ if 20 dB $\le A_{min} \le$ 40 dB; and $2 + (20 - A_{min})$ if $A_{min} < 20$ dB.

A controller that cannot be simulated by SPICE is assigned a high penalty value of fitness (10^8).

3.5 Control Parameters

The population size, M, was 100,000. A (generous) maximum size of 150 points (for functions and terminals) was established for each result-producing branch and a (generous) maximum size of 100 points was established for each automatically defined function. The percentages of the genetic operations for each generation are 46% one-offspring crossover on internal points of the program tree other than numerical constant terminals, 9% one-offspring crossover on points of the program tree other than numerical constant terminals, 9% one-offspring crossover on numerical constant terminals, 1% mutation on points of the program tree other than numerical constant terminals, 20% mutation on numerical constant terminals, 9% reproduction, 2% subroutine creation, 2% subroutine duplication, and 2% subroutine deletion. The other parameters are the same default values that we have used on many other problems (Koza, Bennett, Andre, Keane 1999).

3.6 Termination

The run was manually monitored and manually terminated when the fitness of many successive best-of-generation individuals appeared to have reached a plateau. The best-so-far individual was harvested and designated as the result of the run.

3.7 Parallel Implementation

This problem was run on a home-built Beowulf-style (Sterling, Salmon, Becker, and Savarese 1999) parallel cluster computer system consisting of 1,000 350 MHz Pentium II processors (each accompanied by 64 megabytes of RAM). The system has a 350 MHz Pentium II computer as host. The processing nodes are connected with a 100 megabit-per-second Ethernet. The processing nodes and the host use the Linux operating system. The distributed genetic algorithm with unsynchronized generations and semi-isolated subpopulations was used with a subpopulation size of Q = 100 at each of D = 1,000 demes. As each processor (asynchronously) completes a generation, four boatloads of emigrants from each subpopulation are dispatched to each of the four toroidally adjacent processors. The 1,000 processors are hierarchically organized. There are 5 × 5 = 25 high-level groups (each containing 40 processors). If the adjacent node belongs to a different group, the migration rate is 2% and emigrants are selected based on fitness. If the adjacent node belongs to the same group, emigrants are selected randomly with a 5% migration rate (10% if the adjacent node is in the same physical box).

4 Results

The initial random generation is a blind random search of the search space of the problem. The best-of-generation circuit from generation 0 has a fitness of 14,530.8.

The best-of-run controller (figure 4) appears in generation 217. This genetically evolved controller has an overall fitness of 14.996. The program tree has one result-producing branch with 10 points and five automatically defined functions (with 22, 38, 3, 19, and 3 points, respectively). The result-producing branch refers to `ADF0`. Also, `ADF0` hierarchically refers to `ADF1`. The other three automatically defined functions are not referenced. Note that the controller's output is fed back internally into the controller.

Figure 5 compares the time-domain response of the best-of-run controller (triangles) from generation 217 and the Astrom and Hagglund controller (squares) to a 1-volt reference signal for the three-lag plant. The comparisons for other reference signals, disturbance signals, and plants from the two families are similarly superior (and are not shown for reasons of space).

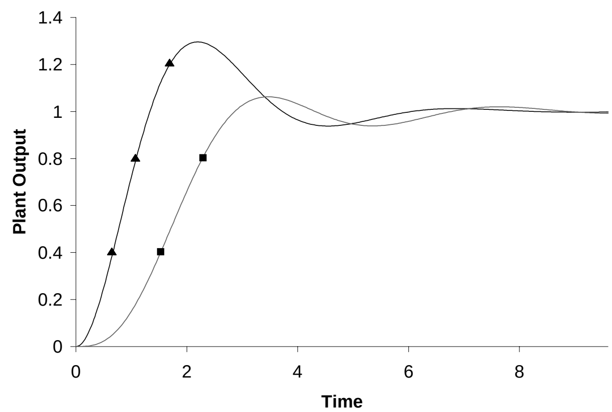

Figure 5 Comparison of time-domain responses.

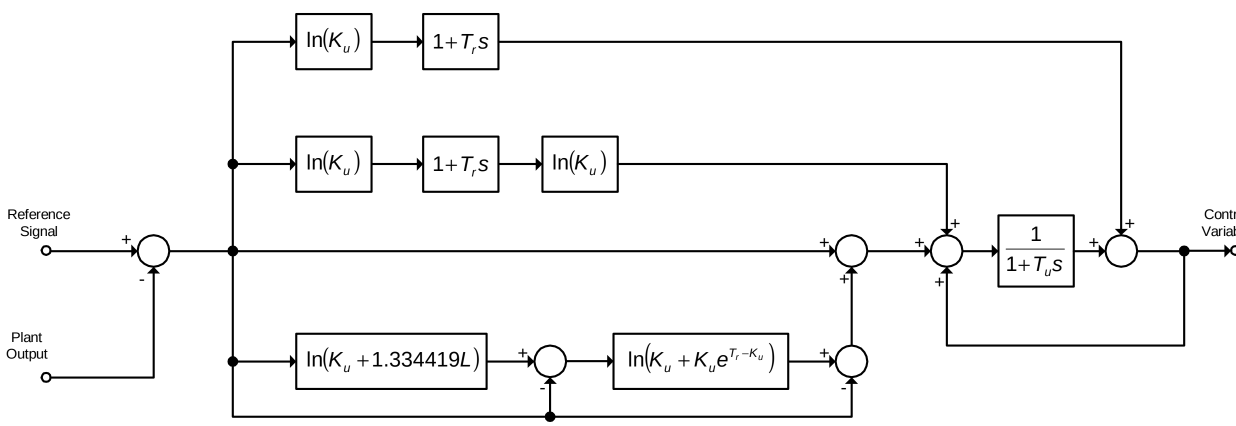

Figure 4 Block diagram of best-of-run controller from generation 217.

Table 2 Control signal, $U(s)$, for the best-of-run controller from generation 217

$$U(s)=\frac{(1+T_r s)(1+T_u s)\ln(K_u)+(1+T_r s)(\ln(K_u))^2+\ln\left(K_u\left(1+e^{T_r-K_u}\right)\right)\left(\ln(K_u+1.334419L)-1\right)}{T_u s}$$

Table 3 Three coefficients of PID controller equivalent to the best-of-run controller from generation 217

$K = \dfrac{\ln(K_u)(T_u + T_r(1+\ln(K_u)))}{T_u}$
$K_d = \ln(K_u)T_r$
$K_i = \dfrac{\ln(K_u)(1+\ln(K_u)) + \left(\ln(K_u) + \ln\left(1+e^{T_r - K_u}\right)\right)\left(\ln(K_u + 1.33419L) - 1\right)}{T_u}$

Table 4 Comparison of characteristics of the controller and the Astrom and Hagglund controller for all six plants

Plant	Plant	Genetically evolved Controller				Astrom and Hagglund Controller			
		ITAE Step	ITAE Disturb	M_s	A_{min}	ITAE Step	ITAE Disturb	M_s	A_{min}
1	$\frac{1}{(1+s)^3}$	1.93	1.15	1.66	41.26	2.75	1.28	2.11	43
2	$\frac{1}{(1+s)^4}$	4.60	6.64	1.80	54.17	8.5	7.6	2.08	58
3	$\frac{1}{(1+s)^8}$	27.43	74.20	1.69	85.8	49.7	78	1.87	90
4	$\frac{1}{(1+s)(1+0.2s)(1+0.2^2s)(1+0.2^3s)}$	0.037	0.0055	1.59	35.23	0.051	0.006	1.9	40
5	$\frac{1}{(1+s)(1+0.5s)(1+0.5^2s)(1+0.5^3s)}$	0.436	0.498	1.72	47.5	0.945	0.522	2.07	50
6	$\frac{1}{(1+s)(1+0.7s)(1+0.7^2s)(1+0.7^3s)}$	1.40	1.99	1.77	52.2	2.9	2.23	2.07	55

Figure 6 compares the time-domain response of the best-of-run controller (triangles) from generation 217 and the Astrom and Hagglund controller (squares) to a 1-volt disturbance signal for the three-lag plant. The comparisons for other reference signals, disturbance signals, and plants from the two families are similarly superior.

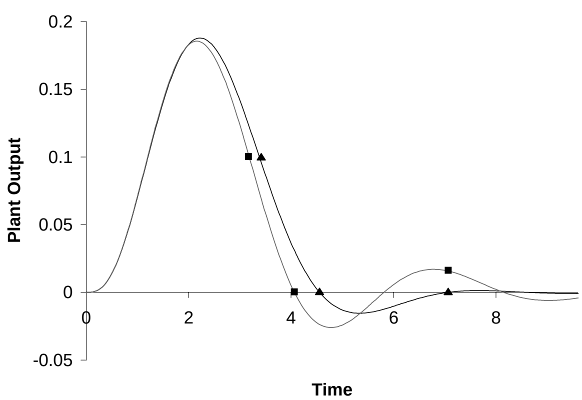

Figure 6 Comparison of the disturbance responses.

Table 2 presents the control signal, $U(s)$, for the best-of-run controller from generation 217. Note that all four parameters (K_u, T_u, T_r, and L) appear.

When simplified, it can be seen that the best-of-run controller from generation 217 is a PID controller whose three coefficients are as shown in table 3.

Table 4 compares the characteristics of the best-of-run controller from generation 217 with those of the Astrom and Hagglund (1995) controller for all six plants. As can be seen, the genetically evolved controller is superior to the Astrom and Hagglund controller for all six plants for the integral of the time-weighted absolute error (ITAE) for the step input, the ITAE for disturbance rejection, and the maximum sensitivity, M_s. All values of A_{min} are above the required minimum 40 (except for plant 4). Averaged over the six plants, the ITAE for the step input for the genetically evolved controller is only 58% of the value for the Astrom and Hagglund controller; the ITAE for disturbance rejection is 91% of the value for the Astrom and Hagglund controller; and the maximum sensitivity, M_s. for the genetically evolved controller is only 85% of the value for the Astrom and Hagglund controller.

The PID controller was a significant improvement over previous approaches to control. As Callender and Stevenson state in their 1939 patent,

> "A specific object of the invention is to provide a system which will produce a compensating effect governed by factors proportional to the total extent of the deviation, the rate of the deviation, and the summation of the deviation during a given period …"

Claim 1 of Callender and Stevenson (1939) covers what is now called the PI controller,

> "A system for the automatic control of a variable characteristic comprising means proportionally responsive to deviations of the characteristic from a desired value, compensating means for adjusting the value of the characteristic, and electrical means associated with and actuated by responsive variations in said responsive means, for operating the compensating means to correct such deviations in conformity with the sum of the extent of the deviation and the summation of the deviation."

Claim 3 of Callender and Stevenson (1939) covers what is now called the PID controller,

> "A system as set forth in claim 1 in which said operation is additionally controlled in conformity with the rate of such deviation."

The legal criteria for obtaining a U. S. patent are that the proposed invention is "new" and "useful" and

> "... the differences between the subject matter sought to be patented and the prior art are such that the subject matter as a whole would [not] have been obvious at the time the invention was made to a person having ordinary skill in the art to which said subject matter pertains." (35 *United States Code* 103a).

Patents are only issued if an arms-length examiner is convinced that the proposed invention is novel, useful, and satisfies the statutory test for unobviousness. Since filing for a patent entails the expenditure of a considerable amount of time and money, patents are generally sought only if the invention is likely to prove useful in the real world. Certainly the PID controller has proved useful since PD, PI, and PID controllers are in widespread use in industry throughout the world.

The fact that genetic programming rediscovered both the topology and sizing of a controller that was unobvious "to a person having ordinary skill in the art" establishes that this evolved result satisfies Arthur Samuel's criterion (1983) for artificial intelligence and machine learning, namely

> "The aim [is] ... to get machines to exhibit behavior, which if done by humans, would be assumed to involve the use of intelligence."

The values of the PID coefficients of the controller created by genetic programming are very close to those of the Astrom and Hagglund (1995) controller.

Most of the computer time was consumed by the fitness evaluation of candidate individuals in the population. The fitness evaluation (involving 36 time-consuming time-domain SPICE simulations and 12 relatively fast frequency-domain SPICE simulations) averaged about 6.7 seconds per individual (using a 350 MHz Pentium II processor). The best-of-run individual from generation 217 was produced after evaluating 2.18×10^7 individuals. This required 40.58 hours on our 1,000-node parallel computer system — that is, the expenditure of 5.11×10^{16} computer cycles (about 51 peta-cycles of computer time).

The four parameters (K_u, T_u, T_r, and L) in the above automatically created result are free variables. A mathematical formula containing one or more free variables is "general" in the sense that it provides a solution to an entire category of problems. For example, the familiar formula for solving a quadratic equation contains free variables representing the coefficients of the equation. Here genetic programming has automatically created a "general" solution to an entire category of problems (i.e., all the plants in the two families) — not merely a single instance of the problem (i.e., a particular single plant).

5 Conclusion

This paper demonstrated that genetic programming can be used to automatically create the design for both the topology and parameter values (tuning) for a single common controller (containing various parameters representing the overall characteristics of the plant) for two families of plants. The genetically evolved controller outperforms the controller designed with conventional techniques. The genetically evolved controller is "general" in the sense that it provides a solution that is applicable to all the plants in the two families — not merely a particular single plant).

References

Astrom, Karl J. and Hagglund, Tore. 1995. *PID Controllers: Theory, Design, and Tuning.* Second Edition. Research Triangle Park, NC: Instrument Society of America.

Banzhaf, Wolfgang, Daida, Jason, Eiben, A. E., Garzon, Max H., Honavar, Vasant, Jakiela, Mark, and Smith, Robert E. (editors). 1999. *GECCO-99: Proceedings of the Genetic and Evolutionary Computation Conference, July 13-17, 1999, Orlando, Florida USA*. San Francisco, CA: Morgan Kaufmann.

Banzhaf, Wolfgang, Nordin, Peter, Keller, Robert E., and Francone, Frank D. 1998. *Genetic Programming – An Introduction*. San Francisco, CA: Morgan Kaufmann and Heidelberg: dpunkt.

Banzhaf, Wolfgang, Poli, Riccardo, Schoenauer, Marc, and Fogarty, Terence C. 1998. *Genetic Programming: First European Workshop. EuroGP'98. Paris, France, April 1998 Proceedings. Paris, France. April l998*. Lecture Notes in Computer Science. Volume 1391. Berlin, Germany: Springer-Verlag.

Callender, Albert and Stevenson, Allan Brown. 1939. *Automatic Control of Variable Physical Characteristics*. United States Patent 2,175,985. Filed February 17, 1936 in United States. Filed February 13, 1935 in Great Britain. Issued October 10, 1939 in United States.

Gruau, Frederic. 1992. Genetic synthesis of Boolean neural networks with a cell rewriting developmental process. In Schaffer, J. D. and Whitley, Darrell (editors). *Proceedings of the Workshop on Combinations of Genetic Algorithms and Neural Networks 1992*. Los Alamitos, CA: The IEEE Computer Society Press.

Holland, John H. 1975. *Adaptation in Natural and Artificial Systems*. Ann Arbor, MI: University of Michigan Press.

Koza, John R. 1992. *Genetic Programming: On the Programming of Computers by Means of Natural Selection.* Cambridge, MA: MIT Press.

Koza, John R. 1994a. *Genetic Programming II: Automatic Discovery of Reusable Programs.* Cambridge, MA: MIT Press.

Koza, John R. 1994b. *Genetic Programming II Videotape: The Next Generation*. Cambridge, MA: MIT Press.

Koza, John R., Bennett III, Forrest H, Andre, David, and Keane, Martin A. 1999. *Genetic Programming III: Darwinian Invention and Problem Solving*. San Francisco, CA: Morgan Kaufmann.

Koza, John R., Bennett III, Forrest H, Andre, David, Keane, Martin A., and Brave, Scott. 1999. *Genetic Programming III Videotape*: *Human-Competitive Machine Intelligence*. San Francisco, CA: Morgan Kaufmann.

Koza, John R., Keane, Martin A., Yu, Jessen, Bennett, Forrest H III, and Mydlowec, William. 2000. Automatic creation of human-competitive programs and controllers by means of genetic programming. *Genetic Programming and Evolvable Machines*. 1 (1 -2) 121 - 164.

Koza, John R., and Rice, James P. 1992. *Genetic Programming: The Movie*. Cambridge, MA: MIT Press.

Langdon, William B. 1998. *Genetic Programming and Data Structures: Genetic Programming + Data Structures = Automatic Programming!* Amsterdam: Kluwer.

Marenbach, Peter, Bettenhausen, Kurt D., and Freyer, Stephan. 1996. Signal path oriented approach for generation of dynamic process models. In Koza, John R., Goldberg, David E., Fogel, David B., and Riolo, Rick L. (editors). *Genetic Programming 1996: Proceedings of the First Annual Conference, July 28-31, 1996, Stanford University*. Cambridge, MA: MIT Press. Pages 327 - 332.

Poli, Riccardo, Nordin, Peter, Langdon, William B., and Fogarty, Terence C. 1999. *Genetic Programming: Second European Workshop. EuroGP'99. Proceedings*. Lecture Notes in Computer Science. Volume 1598. Berlin: Springer-Verlag.

Quarles, Thomas, Newton, A. R., Pederson, D. O., and Sangiovanni-Vincentelli, A. 1994. *SPICE 3 Version 3F5 User's Manual*. Department of Electrical Engineering and Computer Science, University of California. Berkeley, CA. March 1994.

Ryan, Conor. 1999. *Automatic Re-engineering of Software Using Genetic Programming*. Amsterdam: Kluwer Academic Publishers.

Samuel, Arthur L. 1983. AI: Where it has been and where it is going. *Proceedings of the Eighth International Joint Conference on Artificial Intelligence*. Los Altos, CA: Morgan Kaufmann. Pages 1152 – 1157.

Spector, Lee, Langdon, William B., O'Reilly, Una-May, and Angeline, Peter (editors). 1999. *Advances in Genetic Programming 3*. Cambridge, MA: MIT Press.

Sterling, Thomas L., Salmon, John, Becker, Donald J., and Savarese, Daniel F. 1999. *How to Build a Beowulf: A Guide to Implementation and Application of PC Clusters*. Cambridge, MA: MIT Press.

Wong, Man Leung and Leung, Kwong Sak. 2000. *Data Mining Using Grammar Based Genetic Programming and Applications*. Amsterdam: Kluwer Academic Publishers.

Ziegler, J. G. and Nichols, N. B. 1942. Optimum settings for automatic controllers. *Transactions of ASME*. (64) 759-768.